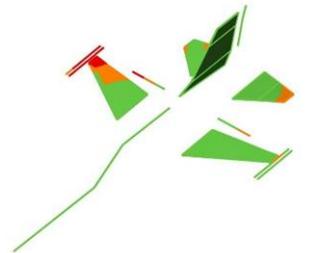
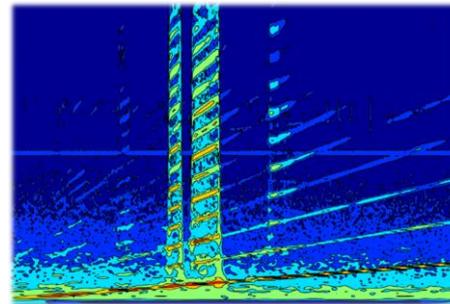


Analysis of the Nonlinear Dynamics of an F-16 Aircraft Using the NI2D Toolbox

T. Dossogne, J.P. Noël, L. Masset,
T. Detroux, G. Kerschen

Space Structures and Systems Lab.
University of Liège, Belgium



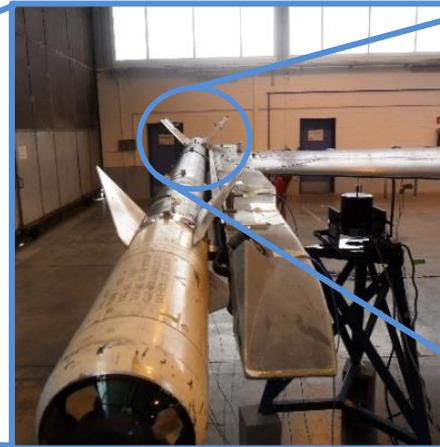
Our Test Case: the F-16 Fighter Aircraft

F-16 fighter aircraft



Saffraanberg,
Belgium.

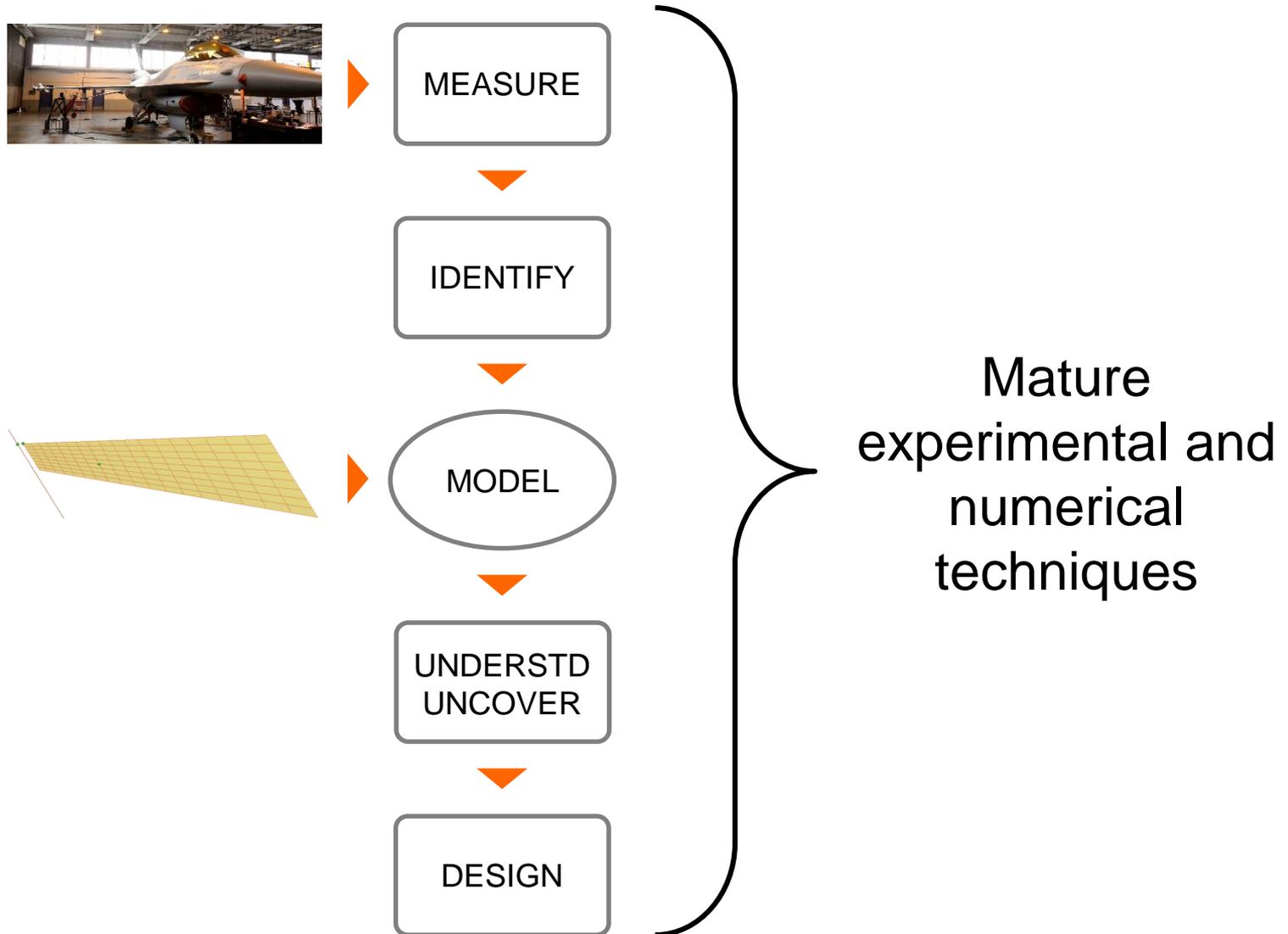
Wing-to-missile
mounting interface



Nonlinear
connection?



Design Cycle of Nonlinear Engineering Structures



Outline



MEASURE



IDENTIFY



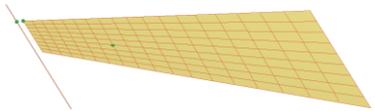
MODEL



UNDERSTD
UNCOVER



DESIGN

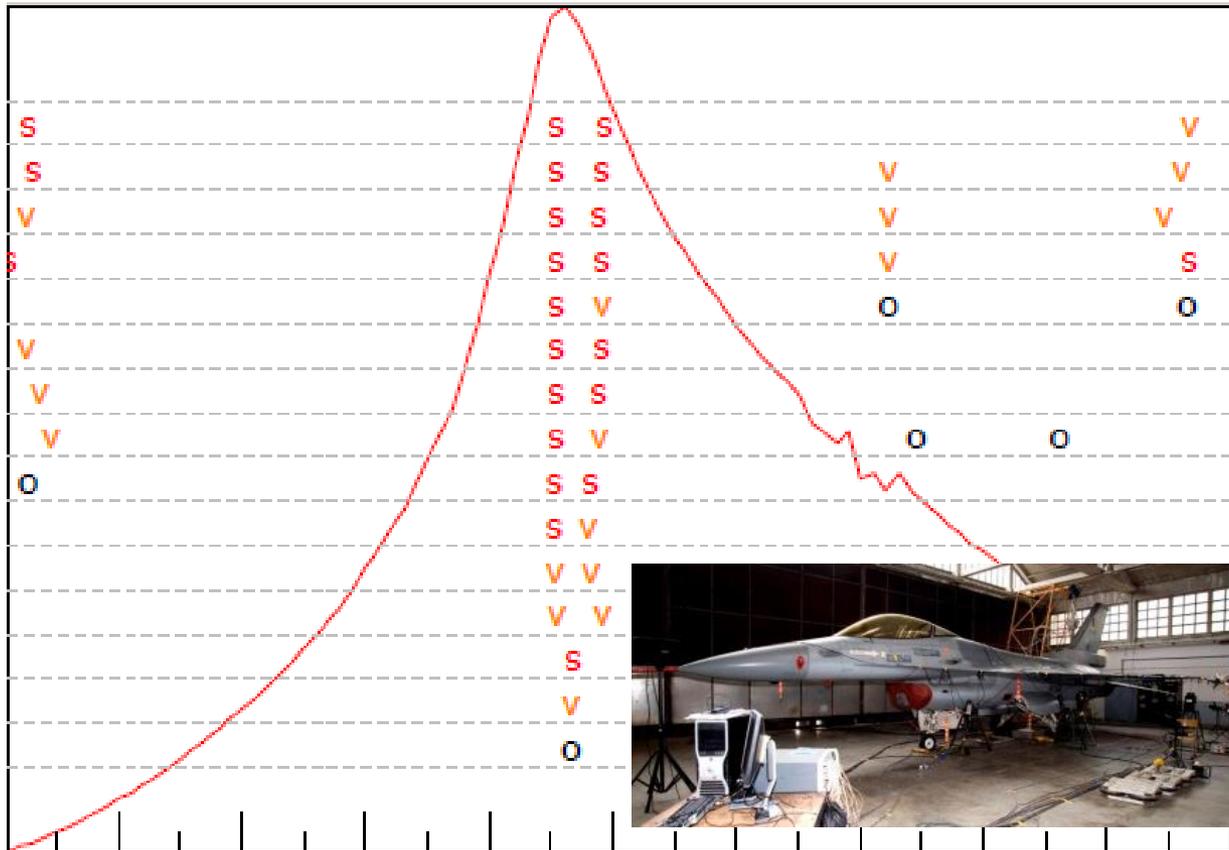


IN THIS
PRESENTATION

Classical Linear Tools May Fail or Give Wrong Results

[B. Peeters et al.,
IMAC 2011]

Model
order



MEASURE

IDENTIFY

MODEL

UNDERSTD
UNCOVER

DESIGN

Evidencing Nonlinearity Is Fairly Straightforward

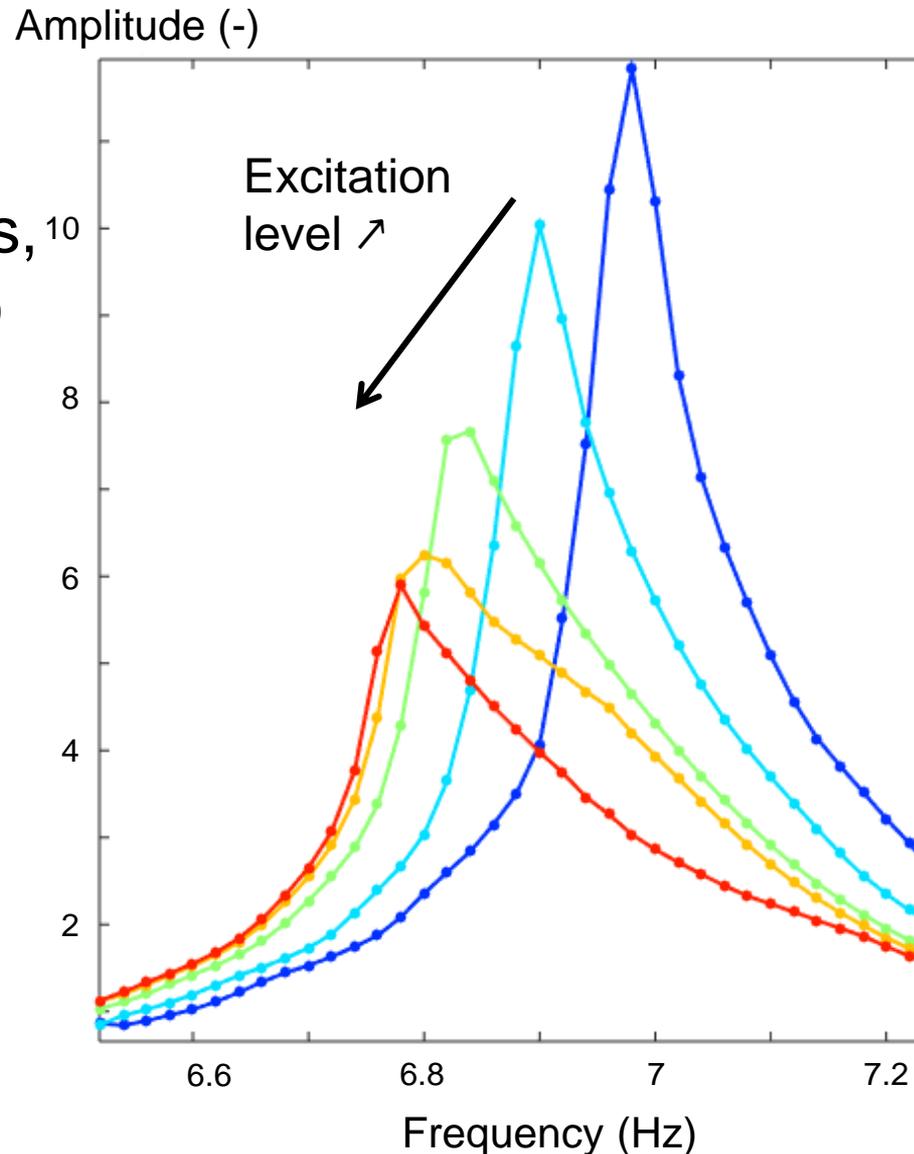
Single FRF:

Distortion (skewness, nonsmoothness, ...) of the resonance peak.

→ usually not applicable with random excitation.

Several levels:

Homogeneity principle can be checked.



MEASURE

IDENTIFY

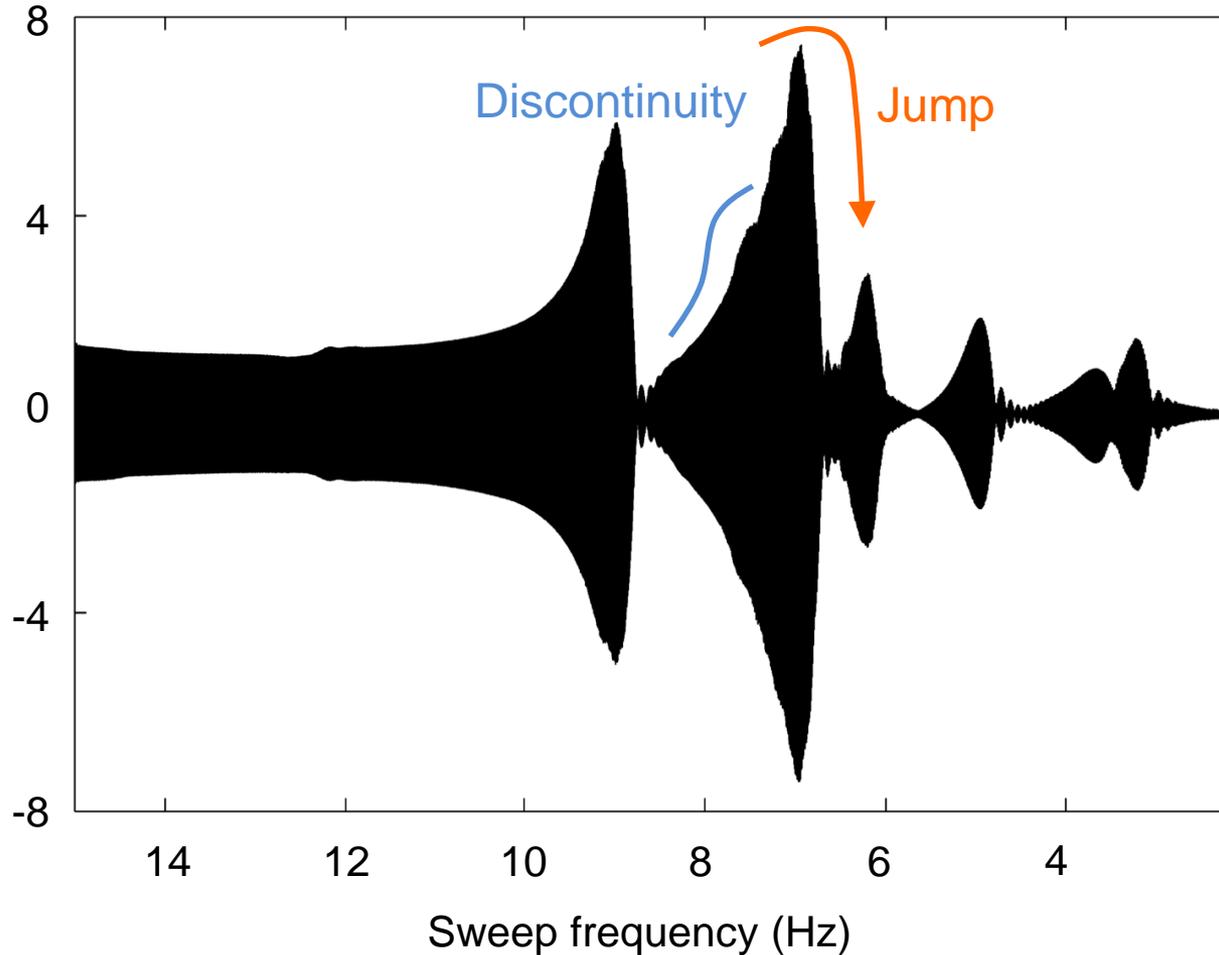
MODEL

UNDERSTD
UNCOVER

DESIGN

Evidencing Nonlinearity Is Fairly Straightforward

Acceleration at missile (m/s²)



MEASURE

IDENTIFY

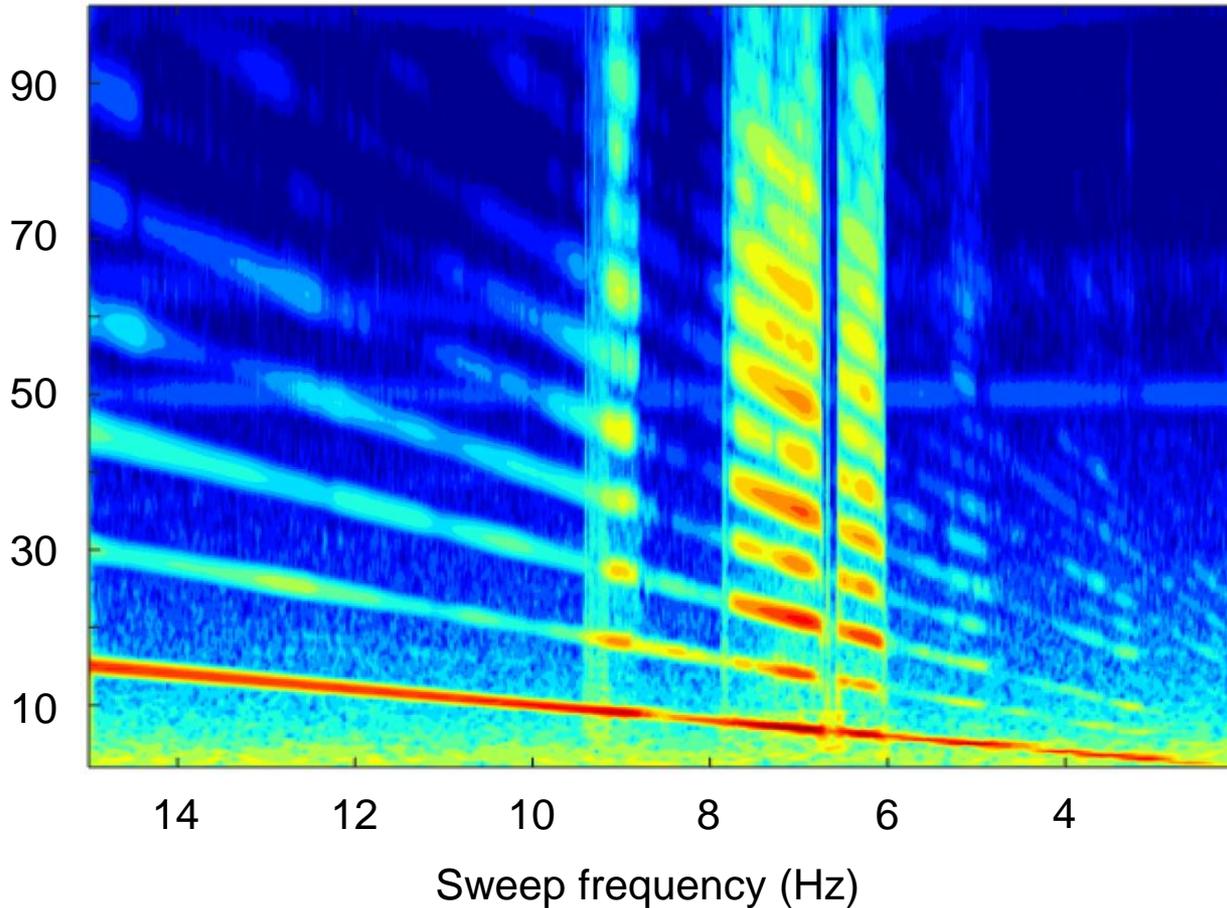
MODEL

UNDERSTD
UNCOVER

DESIGN

Inferring a NL Model from Time-Frequency Analysis

Instantaneous frequency (Hz)



MEASURE

IDENTIFY

MODEL

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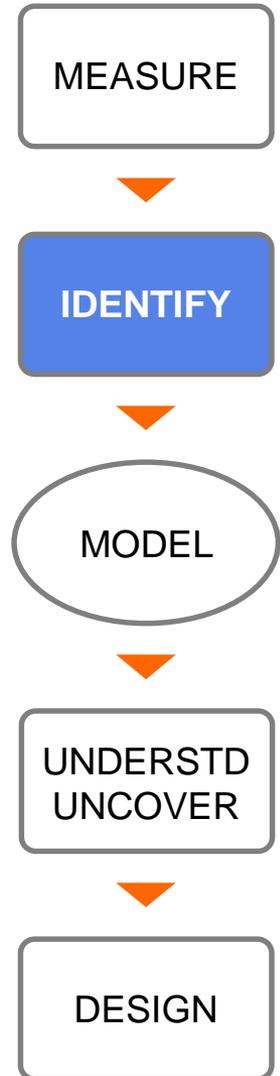
DESIGN

The RFS Method: An Underutilized Approach

Introduced by Masri and Caughey (1979, ASME JAM) as a nonlinear parameter estimation technique.

Very popular in structural dynamics because of its simplicity.

Rigorously applicable to low-dimensional systems, but can be exploited **qualitatively for visualising nonlinearity**.



How Can We Visualize the NL Behavior of this Connection?



Slide connection involving complex dynamics.

Physical insight is key to parametric modelling.

MEASURE



IDENTIFY



MODEL

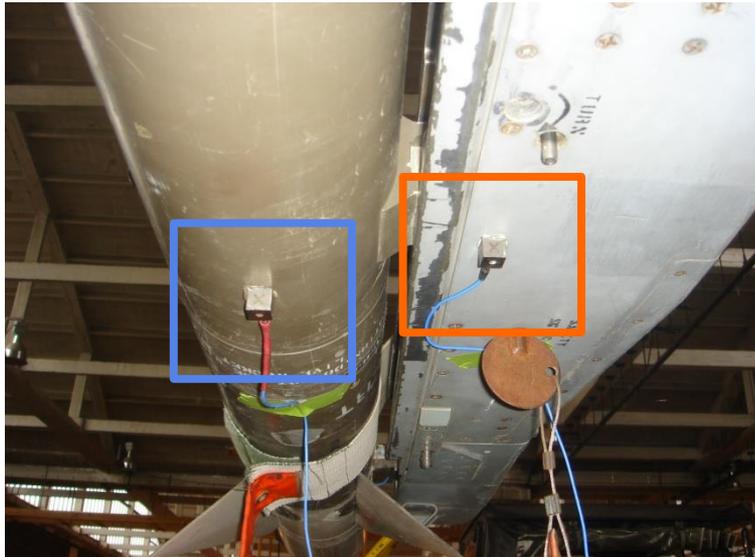
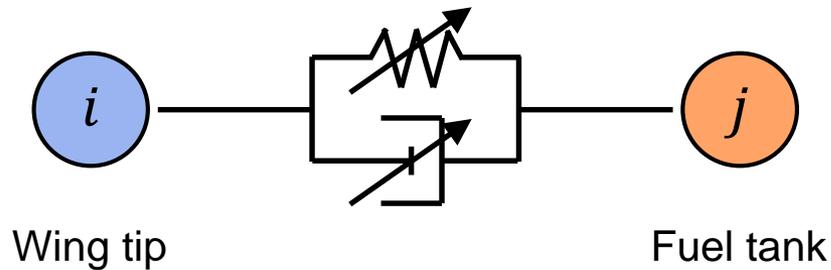


UNDERSTD
UNCOVER



DESIGN

Macroscopic Idealization as Lumped Spring and Dashpot



Potential nonlinear connections must be instrumented on both sides.

MEASURE

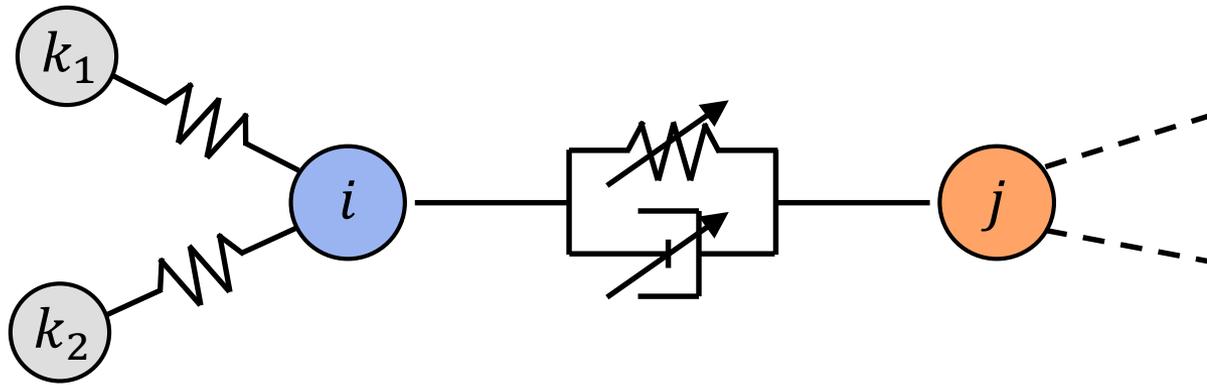
IDENTIFY

MODEL

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Newton's Second Law Written at Degree of Freedom "i"



MEASURE

IDENTIFY

MODEL

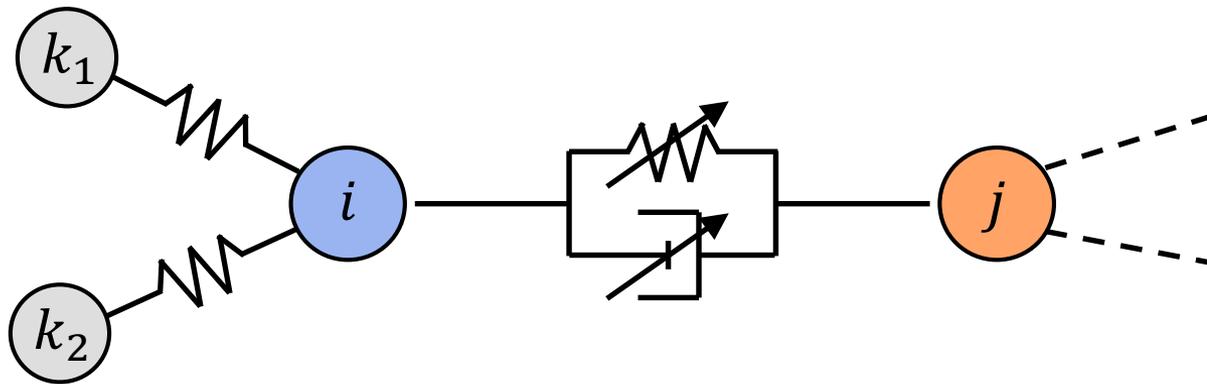
UNDERSTD
UNCOVER

DESIGN

Linear connections
to neighbouring DOFs
(e.g., bending stiffnesses in a wing)

$$\sum_k m_{i,k} \ddot{q}_k + g_i(q, \dot{q}) = p_i$$

Discard all Terms not Related to the Nonlinear Connection



Linear connections
to neighbouring DOFs
(e.g., bending stiffnesses in a wing)

$$\sum_k m_{i,k} \ddot{q}_k + g_i(q, \dot{q}) = p_i$$

$$m_{i,i} \ddot{q}_i + g_i(q_i - q_j, \dot{q}_i - \dot{q}_j) \cong p_i$$

MEASURE

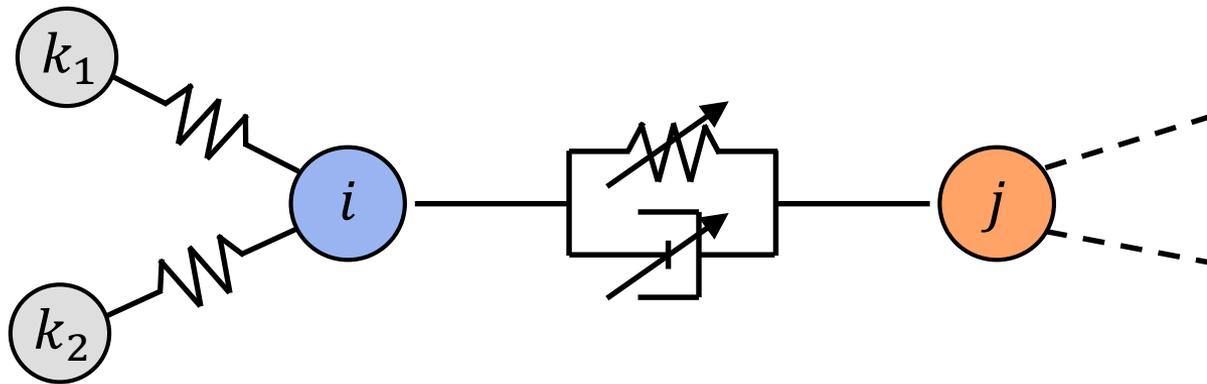
IDENTIFY

MODEL

UNDERSTD
UNCOVER

DESIGN

Assume no Forcing Term and Drop the Mass Constant



Linear connections
to neighbouring DOFs
(e.g., bending stiffnesses in a wing)

$$\sum_k m_{i,k} \ddot{q}_k + g_i(q, \dot{q}) = p_i$$

NL can be
visualized!

$$g_i(q_i - q_j, \dot{q}_i - \dot{q}_j) \cong -\ddot{q}_i$$

MEASURE

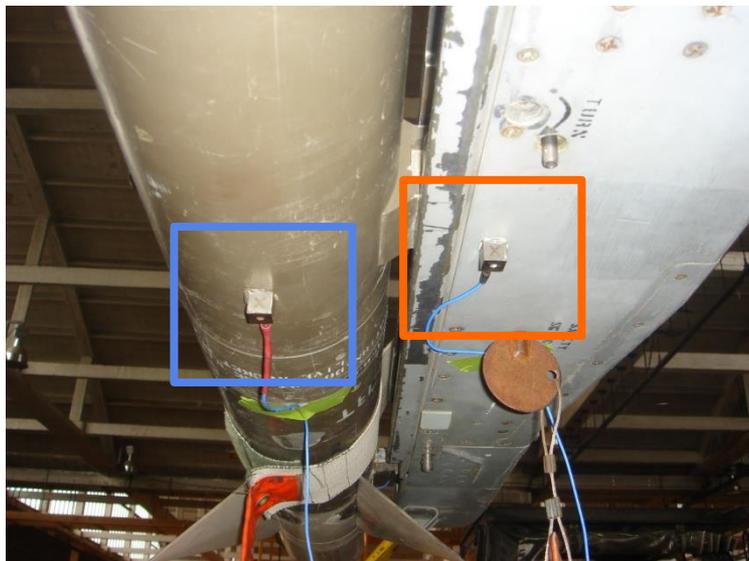
IDENTIFY

MODEL

UNDERSTD
UNCOVER

DESIGN

Demo in NI2D Software



MEASURE



IDENTIFY



MODEL

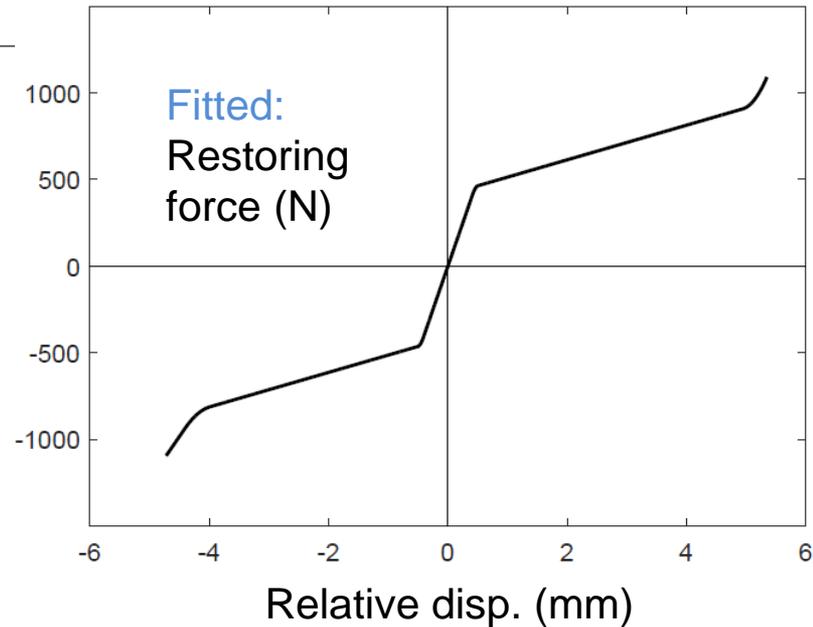
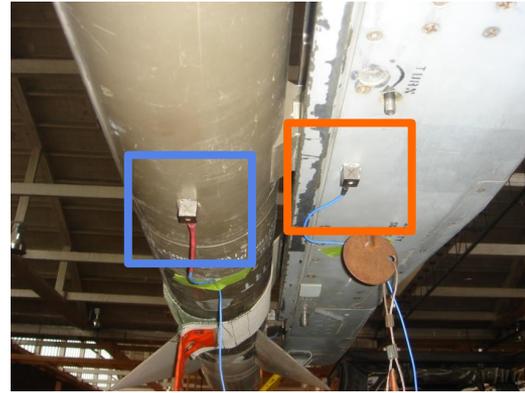
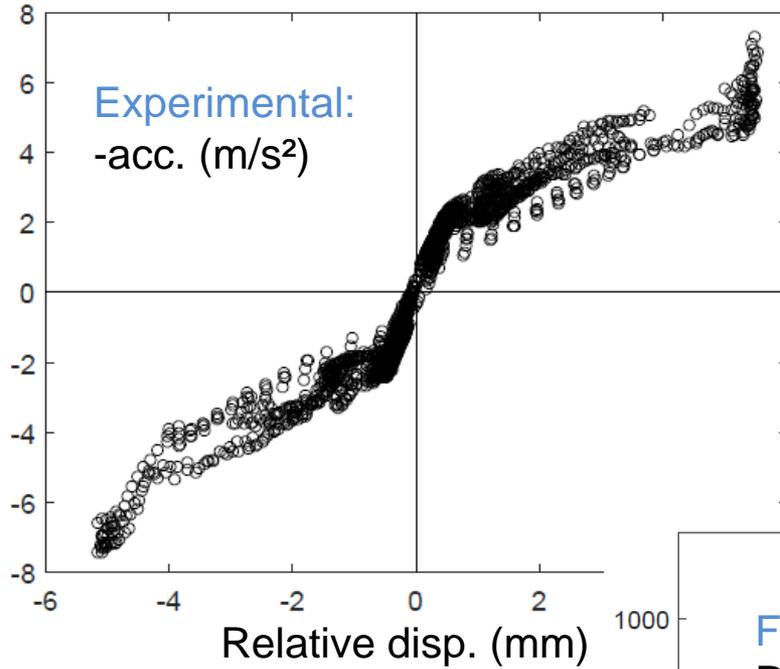


UNDERSTD
UNCOVER



DESIGN

Quantifying the Parameters of the Nonlinearity Model



MEASURE



IDENTIFY



MODEL



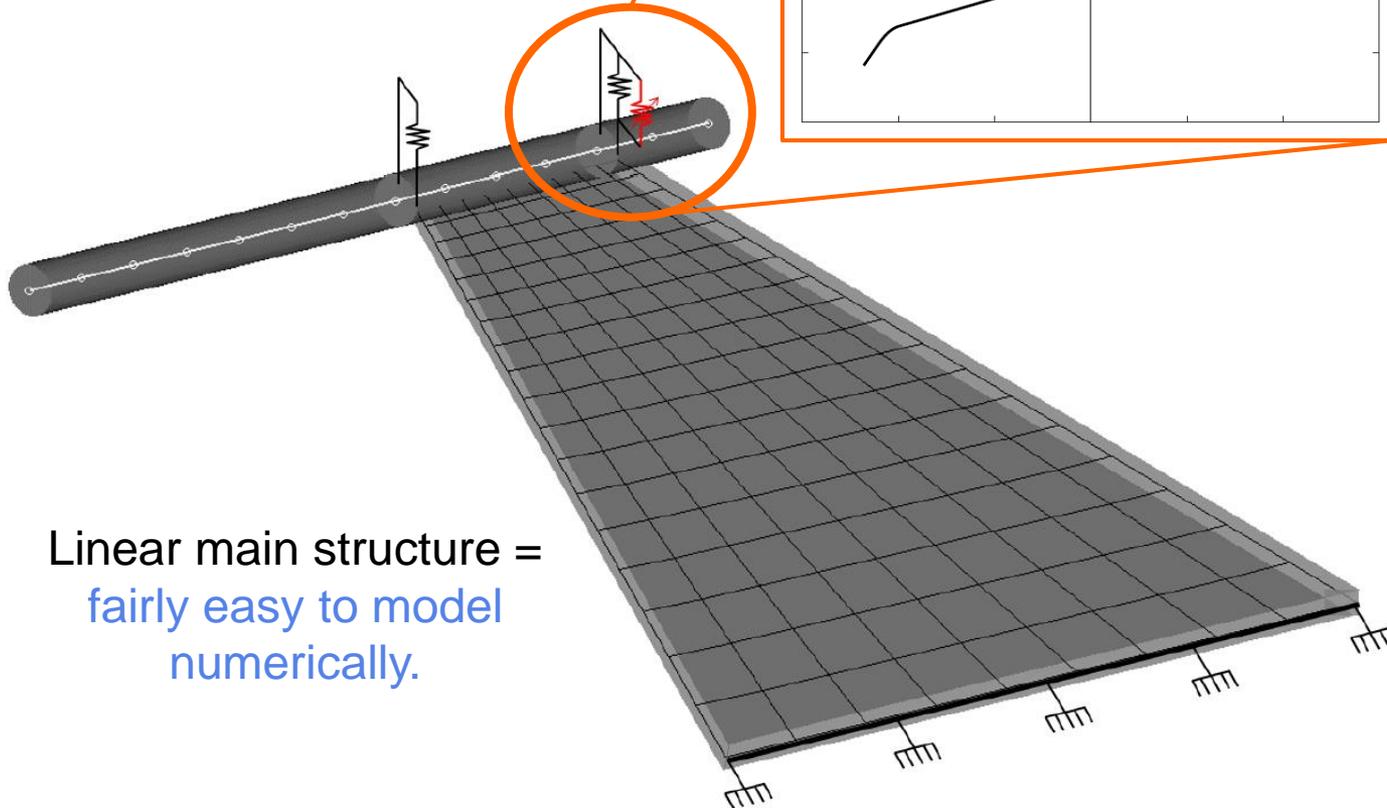
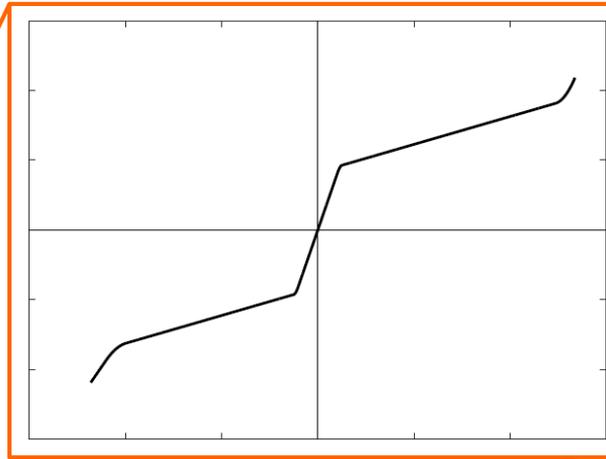
UNDERSTD
UNCOVER



DESIGN

Data-Driven and Computer-Aided Models Are Integrated

Nonlinear component =
difficult to model numerically.



Linear main structure =
fairly easy to model
numerically.

MEASURE



IDENTIFY



MODEL

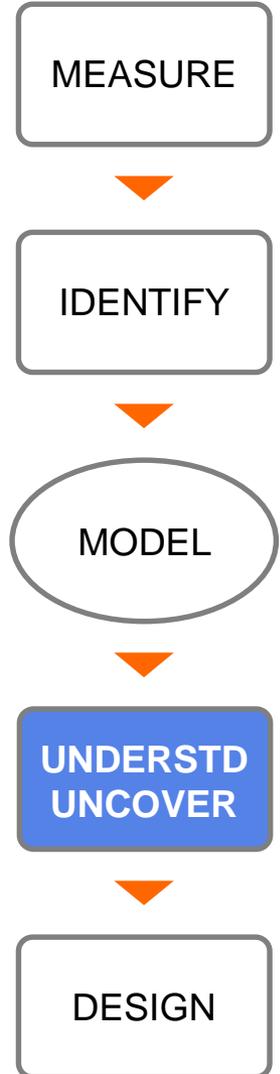


UNDERSTD
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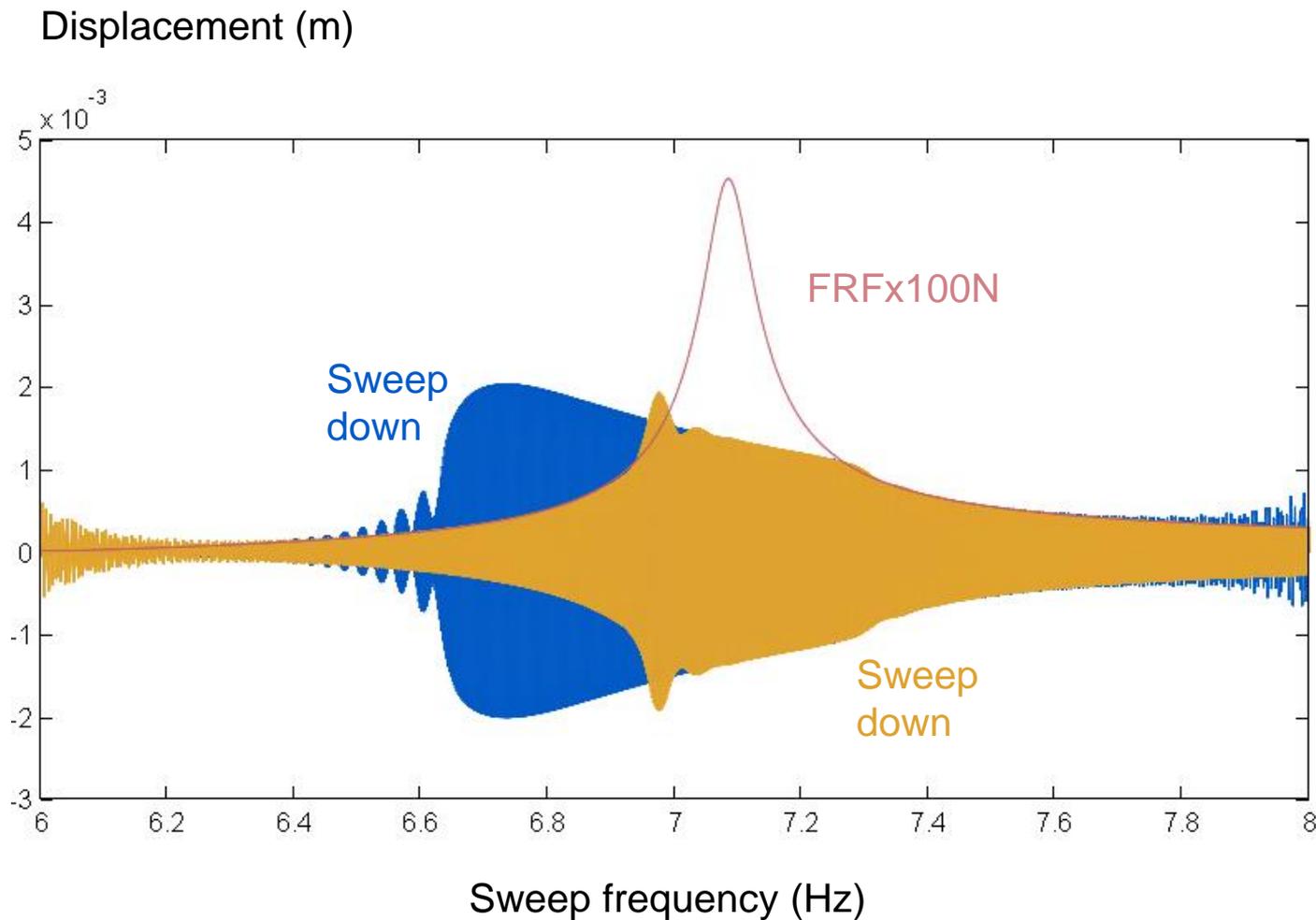


DESIGN

Classical Nonlinear Simulation Tools Can Now Be Employed



Responses to Swept-Sine Excitations



MEASURE

IDENTIFY

MODEL

UNDERSTD
UNCOVER

DESIGN

Concluding Remarks

Data-driven and computer-aided techniques are complementary approaches to model nonlinear structures.

With limited physical insight, a complete design cycle can be studied.

This allows to precisely quantify the impact of nonlinearities, and to undertake design modifications on a sound basis.

Thank you for your attention!

Thibaut Detroux

Space Structures and Systems Lab.
University of Liège, Belgium



NOLISYS
Solutions & Software
for Nonlinear Vibrating Systems