

Une école en mouvement



IN101: Algorithmique et Programmation

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École Nationale Supéri de **Techniques Avanc**

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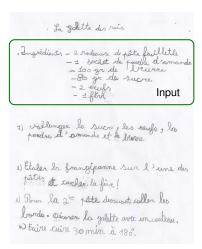
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. La golette des rois Ingrédient, - 2 rodeaux de pâte fuillitée - 1 socht de pouds d'amarde - 500 gr de Neure -80 gr de ruere - 2 seuls - I ferr 1) d'élanger le sucre, les oeufs, la poudre d'amonde et le service. 2) Etaler la frangipanne sur l'une des pates et cacher la fire! 3) Poser la 2 pate dessuset coller les bords. Décorer la galette avec un conteau. 4) Eaire cuire 30 min à 180°.

An algorithm is like a cooking recipe





An algorithm is like a cooking recipe
 Input (80gr de sucre, etc.)





2) Etaler la frangipanne sur l'une des parties et cachen la fine!

3) Poser la 2° parte dossust coller les bords. Oscorer la golette avec un conten.

4) Enire cuire 30 min. à 13 nistructions An algorithm is like a cooking recipe

Input

Instructions

(80gr de sucre, etc.)



. La golette des rois Output

. Ingrédients - 2 rodeaux de pâte failletée - 1 sochet de poudre d'amande - 100 gre de l'eurre -80 gr de sugre Input - I ferr

1) d'élanger le sucre, les oeufs, la poudre d'amonde et le service. 2) Etaler la frangipanne sur l'une des pates et cacher la fire! 3) Poser la 2 = pate dessuset coller les bords. Décorer la golette avec un conteau. 4) Enire cuire 30 min à 18 nstructions

- An algorithm is like a cooking recipe
 - Input
 - (80gr de sucre, etc.) Instructions
 - Output

(galette des rois)



Ingrédient, - 2 relieux de pôte failletée - 1 socht de partie d'amande - 100 gar de l'eure - 20 gar de sucre - 2 seefs - 1 flut

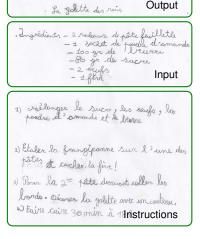
2) Staler la frangipanne sur l'une des partes et a l'une l'enne l'enne des partes et a l'une des partes et accher la fire!

3) Pour la 2° parte docuper soller les bords. aponer la goltte avec un centeau, « D'Enira cuire 30 min à 17 nistructions

- An algorithm is like a cooking recipe
 - 1 Input (80gr de sucre, etc.)
 - Instructions
 - Output (galette des rois)

- Example from computer science
 - sorting ("tri")





- An algorithm is like a cooking recipe
 - Input

(80gr de sucre, etc.)

- Instructions
- Output

(galette des rois)

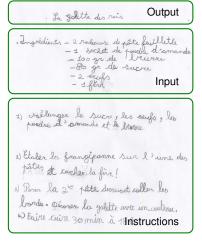
- Example from computer science
 - sorting ("tri")

Input:

5

4

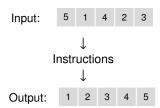
2



An algorithm is like a cooking recipe
Input (80gr de sucre, etc.)
Instructions
Output (galette des rois)

Example from computer science

sorting ("tri")





Instructions

Go through all positions from front to back and do the following:

<u>Find</u> the number with the smallest value starting after the current position <u>Swap</u> that smallest number with the number in the current position

5 1 4 2 3



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Instructions

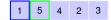
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Instructions

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Instructions

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Instructions

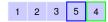
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Instructions

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Instructions

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Instructions

Go through all positions from front to back and do the following:

Find the number with the smallest value starting after the current position

Swap that smallest number with the number in the current position

1 2 3 4 5



Instructions

Go through all positions from front to back and do the following:

Find the number with the smallest value starting after the current position Swap that smallest number with the number in the current position

You call a sorting algorithm dozens of times a day!



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Instructions

<u>Go</u> through all positions from front to back and do the following:

Find the number with the smallest value starting after the current position

Swap that smallest number with the number in the current position

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Instructions

Go through all positions from front to back and do the following:

- You call a sorting algorithm dozens of times a day!
 - It is not magic... somewhere, a sorting algorithm is doing the work





Instructions

Go through all positions from front to back and do the following:

Find the number with the smallest value starting after the current position

Swap that smallest number with the number in the current position

- You call a sorting algorithm dozens of times a day!
 - It is not magic... somewhere, a sorting algorithm is doing the work
 - Algorithms automate repetitive work, if we program them





What is programming?

- Represent algorithms in a formal language that
 - Humans can (learn to) understand and write
 - · Computers can read and execute
- Example languages: C, C++, Java, Matlab, Python



What is programming?

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```
# Finding the smallest number
 in a list of numbers in Python
# Input
an_{input} = [8, 9, 6, 5]
print(an_input)
# Instructions
smallest = an_input[0]
for number in an_input:
    if (number < smallest):</pre>
        smallest = number
# Output
output = smallest
print(output)
```

Example Algorithm: Inceptionism

"Inceptionism: Going Deeper into Neural Networks"

http://googleresearch.blogspot.co.uk/2015/06/inceptionism-going-deeper-into-neural.html

- Neural networks that dream!
- So what do they dream? Example...





Outline

- Algorithms
- Programming
- Cours IN101
 - Why IN101?
 - Objectives
 - Modalités
- Python Basics
- 5 TD



Automation is everywhere!

⇒ Algorithms are everywhere!

- Many programs are called every time you:
 - do an Internet search
 - use your smartphone
 - drive your car







Automation is everywhere!

⇒ Algorithms are everywhere!

- Many programs are called every time you:
 - do an Internet search
 - use your smartphone
 - drive your car (even more if your car drives by itself!)









Automation is everywhere!

⇒ Algorithms are everywhere!

 \Rightarrow Programming is everywhere!





Automation is everywhere!

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Automation is everywhere!

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Automation is everywhere!

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Automation is everywhere!

⇒ Algorithms are everywhere!

⇒ Programming is everywhere!



ENSTA ENSTA





ENSTA Group





Automation is everywhere!

⇒ Algorithms are everywhere!

⇒ Programming is everywhere!

Two robots cooking pancakes, with algorithms written in Python and C++.





IN101 Algorithmique et Programmation: Objectives

- Objectives are to learn to
 - formulate algorithms from problem descriptions
 - implement algorithms in a programming language
 - the programming language being Python
 - · apply several common algorithms in computer science
 - formulate and implement algorithms autonomously



IN101 Algorithmique et Programmation: Objectives

- Objectives are to learn to
 - formulate algorithms from problem descriptions
 - implement algorithms in a programming language
 - the programming language being Python
 - apply several common algorithms in computer science
 - formulate and implement algorithms autonomously
- Objectives are not to learn
 - how algorithms/programs are executed on a computer (→ IN102)
 - all features of Python (→ https://docs.python.org/)
 - all programming concepts (→ IN102, IN103, IN104, IN204)



IN101 Modalites

- Main source of information is DFR website:
 - http://wwwdfr.ensta.fr/Cours/index.php?usebdd=ensta&sigle=IN101
 - Schedule, links to books, links to PDFs of CM and TDs.





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- Every week
 - 15:15 ≈16:15 "cours magistral"
 - 15 minute break
 - ≈16:30 18:30 "travaux dirigés"
 - programming autonomously, exercises





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 - 15:15 ≈16:15 "cours magistral"
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 - programming autonomously, exercises
- Contrôle de connaissances, marks

50% 1 graded TD 50% TD8, 15.11.2016





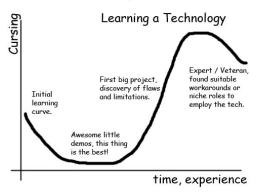
Who are we?

- Cours magistraux (+ travaux dirigés)
 - Vladimir Paun
 - Research topics: formal methods, hard real-time system verification, WCET
 - · Nationality: Romanian
 - · Email: paun@ensta-paristech.fr
 - Office: R.3.28 UIIS, ENSTA ParisTech



Who are you?

- Up until 2 years ago, 90% of the students that arrived at ENSTA had never programmed before
- But you have all (?) had Python in your "prépa"
 - but we don't know at all how well you learned it...





Who are you?

- Up until 2 years ago, 90% of the students that arrived at ENSTA had never programmed before
- But you have all (?) had Python in your "prépa"
 - but we don't know at all how well you learned it...
- Our strategy
 - If you don't know Python at all: we want you to be able to learn
 - "Basic" part of the TD
 - If you are already a hacker: we don't want to bore you
 - "Advanced" part of the TD (you can skip "Basic", if you want)
 - "Everyone" part of the TD: for everyone
- Please give us your (constructive) feedback!



Outline

- Algorithms
- Programming
- Cours IN101
- Python Basics
 - Python Interpreter
 - Variables
 - Operators
 - Control flow
 - Ancient algorithms still used today
- 5 TD



Programming

- Programming: represent algorithms in a formal language that
 - Humans can (learn to) understand and write
 - Computers can read and execute
- Example languages: C, C++, Java, Matlab, Python



Programming

- Programming: represent algorithms in a formal language that
 - · Humans can (learn to) understand and write
 - · Computers can read and execute
- Example languages: C, C++, Java, Matlab, Python
- Why Python in IN101?
 - · easy to learn
 - emphasizes readability
 - multiple programming paradigms
 - fun!
 - · you already know it from the prépa



Origins of Python



Guido van Rossum – "in December 1989, I was looking for a "hobby" programming project that would keep me occupied during the week around Christmas."

Name from "Monty Python's Flying Circus"





Core philosophy: "The Zen of Python"

- · Beautiful is better than ugly
- Explicit is better than implicit
- Simple is better than complex
- Complex is better than complicated

Origins of Python



Guido van Rossum – "in December 1989, I was looking for a "hobby" programming project that would keep me occupied during the week around Christmas."

Name from "Monty Python's Flying Circus"





Core philosophy: "The Zen of Python"

- Préfèrer le beau au laid,
- · l'explicite à l'implicite,
- le simple au complexe,
- le complexe au compliqué,

And now for something completely different...



let's write some programs in Python!



"Hello World" in the Python language

- Put the following in a file helloworld.py
 - · Called a "Python script"

```
print("Hello World!")
```



"Hello World" in the Python language

- Put the following in a file helloworld.py
 - · Called a "Python script"

```
print("Hello World!")
```

- Execute the instructions in the script in a terminal
 - Calls the "Python interpreter"
 - Interprets the instructions and executes them one by one
 - "Reads" from top to bottom

commline> python3 helloworld.py Hello World!



Comments in Python

- Comments
 - Everything on a line following # (le dièze)
 - Ignored by the Python interpreter
 - Intended only for humans reading the script
- Why comments?
 - Documentation: explaining the code

```
# This is a Python script that will print
# "Hello World"
print("Hello World!")
```

commline> python3 helloworldcomments.py Hello World!



Summary

- Python is a programming language
- The Python interpreter...
 - is called from the command line (in a terminal)
 - interprets a Python script from top to bottom
 - executes the instructions in the script
 - ignore comments (everything after a #)



Summary

- Python is a programming language
- The Python interpreter...
 - is called from the command line (in a terminal)
 - interprets a Python script from top to bottom
 - · executes the instructions in the script
 - ignore comments (everything after a #)
- Writing a Python script



Outline

- **Algorithms**
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- Variables in mathematics
 - Character which is not fully specified, or unknown
 - Example: $f(x) = x^2$ (what is the value of the variable x?)
- Variables in computer science and programming are different...



- Variables (in computer science/programming)
 - A name/indentifier ("a") associated with a value ("1")
 - Assignment: associating a variable with a value ("a = 1")
 - The value of a variable can change



```
a = 1  # Assign value '1' to variable with name 'a'
print(a)
```

```
commline> python3 variables1.py
1
```



- Variables (in computer science/programming)
 - A name/indentifier ("a") associated with a value ("1")
 - Assignment: associating a variable with a value ("a = 1")
 - The value of a variable can change



```
a = 1
         # Assign value '1' to variable with name 'a'
print(a)
a = 7
         # Assign a new value to variable 'a'
print(a)
```

```
commline> python3 variables1.py
1
7
```



- Variables (in computer science/programming)
 - A name/indentifier ("a") associated with a value ("1")
 - Assignment: associating a variable with a value ("a = 1")
 - The value of a variable can change



```
a = 1
         # Assign value '1' to variable with name 'a'
print(a)
a = 7
         # Assign a new value to variable 'a'
print(a)
b = 3
         # Assign value '3' to variable with name 'b'
print(b)
```

```
commline> pvthon3 variables1.pv
1
3
```

- Variables (in computer science/programming)
 - A name/indentifier ("a") associated with a value ("1")
 - Assignment: associating a variable with a value ("a = 1")
 - The value of a variable can change



```
a = 1
         # Assign value '1' to variable with name 'a'
print(a)
a = 7
         # Assign a new value to variable 'a'
print(a)
b = 3
         # Assign value '3' to variable with name 'b'
print(b)
b = a * b  # Assign value 'a*b' (=7*3) to variable with name 'b'
print(b)
```

```
commline> pvthon3 variables1.pv
1
3
21
```

Different types of variables

What types of variables are there? Some examples

```
Numbers – whole numbers or real numbers
Boolean – either True or False
Strings – sequence of characters
```

```
whole_number = 1
real_number = 1.540
boolean = True
string = "Hello world"
print(whole_number)
print(real_number)
print(boolean)
print(string)
```

```
commline> python3 variables2.py
1
1.54
True
Hello world
```

Different types of variables

What types of variables are there? Some examples

```
Numbers – whole numbers or real numbers
Boolean - either True or False
  Strings – sequence of characters
```

Determine variable type with type()

```
whole number = 1
real number = 1.540
boolean = True
       = "Hello world"
strina
print(type(whole_number)) # integer
print(type(real_number)) # float
                   # bool
print(type(boolean))
print(type(string))
                         # str
```

```
commline> python3 variables3.py
<class 'int'>
<class 'float'>
<class 'bool'>
<class 'str'>
```

Different types of variables

What types of variables are there? Some examples

```
Numbers – whole numbers or real numbers
Boolean - either True or False
  Strings – sequence of characters
```

- Determine variable type with type()
- 'Typing' discussed in detail in IN102

```
whole number = 1
real number = 1.540
boolean
       = True
       = "Hello world"
strina
print(type(whole_number)) # integer
print(type(real_number)) # float
                   # bool
print(type(boolean))
print(type(string))
                         # str
```

```
commline> python3 variables3.py
<class 'int'>
<class 'float'>
<class 'bool'>
<class 'str'>
```

• Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)

- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =

```
a = 1 # Assignment operator
print(a)
a = 3 # Assignment operator
print(a)
```

```
commline> python3 operators1.py
```



- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * /

```
a = 4 + 3
                # Addition
print(a)
print( 4 - 3 ) # Subtraction
print( 4 * 3 ) # Multiplication
print( 4 / 3 ) # Division
print( 4 ** 3 ) # To the power of
```

```
commline> python3 operators2.py
12
1.3333333333333333
```

- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * / ** %

```
# Division
print( 9  / 2 ) # => 4.5 (float)
print( 9  // 2 ) # => 4  (int)

# Remainder (modulo operator)
print( 9 % 9 )
print( 9 % 7 )
```

```
commline> python3 operators4.py
4.5
4
0
2
```

- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * / ** %
 - Comparison Operators: == ! = < > <= >=

```
print( 4 == 3 ) # Equal?
print( 4 != 3 ) # Not equal?
print( 4 < 3 ) # Smaller than?</pre>
print( 4 > 3 ) # Larger than?
a = (4==3) # Assign result of operator
           # to variable with name 'a'
print(a)
```

```
commline> python3 operators3.py
False
True
False
True
False
```

- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * / ** %
 - Comparison Operators: == ! = < > <= >=
 - Logical Operators: and or not

```
print(1>0 and 1>2)
                   # Both true: No...
print( 1>0 or 1>2 ) # One of them true: Yes!
print( not (1>0 and 1>2) ) # Not true that both are true? Yes!
print( not not 1>0 )
                      # Double negation
```

```
commline> python3 operators5.py
False
True
True
True
```

- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * / ** %
 - Comparison Operators: == ! = < > <= >=
 - · Logical Operators: and or not
- Expression: valid combination of value, variables and operators
 - Examples: 23 23+4 23+a 2*(23+a)
 - Examples: True True and (1>0)



- Returns a value when evaluated (e.g. 4 + 3 evaluates to 7)
 - Assignment Operators: =
 - Arithmetic Operators: + * / ** %
 - Comparison Operators: == ! = < > <= >=
 - · Logical Operators: and or not
- Later in IN101
 - Formal definition
 - Membership and Identity Operators
 - += -= *= /= **=
 - Operators are actually functions (CM02)



Summary

- Variables are names associated with values
- Variables and values may be combined with operators
 - this yields expressions, which themselves yield values



Control flow

Outline

- **Algorithms**
- Programming
- Cours IN101
- **Python Basics**
 - Python Interpreter
 - Variables
 - Operators
 - Control flow
 - Ancient algorithms still used today
- TD



Outline: Control Flow

- of for loop ("boucle for")
- conditional execution ("alternatives")
- while loop ("boucle tant que")



Control Flow: for loop ("boucle for")

What if you want to execute the same instruction several times?

```
number = 0
print(7 * number)
number = 1
print(7 * number)
number = 2
print(7 * number)
number = 3
print(7 * number)
```

```
commline> python3 forloop0.py
14
```



Control Flow: for loop ("boucle for")

- What if you want to execute the same instruction several times?
- for loop: assigns values in a list to a variable, one after the other

```
number = 0
print(7 * number)
number = 1
print(7 * number)
number = 2
print(7 * number)
number = 3
print(7 * number)
```

```
for number in [0, 1, 2, 3]:
    print(7 * number)
```

```
commline> python3 forloop0.py
0
7
14
21
```

```
commline> python3 forloop1.py
0
7
14
21
```

Control Flow: for loop ("boucle for")

- What if you want to execute the same instruction several times?
- for loop: assigns values in a list to a variable, one after the other
- range() function (→ CM2) generates sequences of numbers
 - Careful, range(n1,n2) stops at n2-1
 - range(n) starts at 0 and stops at n-1

```
number = 0
print(7 * number)
number = 1
print(7 * number)
number = 2
print(7 * number)
number = 3
print(7 * number)
```

```
for number in [0, 1, 2, 3]:
    print(7 * number)
for number in range(0, 4):
    print(7 * number)
for number in range(4):
    print(7 * number)
```

```
commline> python3 forloop0.py
0
14
21
```

```
commline> python3 forloop2.py
0
14
21
```

Indentation and code blocks

Indentation is very important in Python



Indentation is very important in Python

```
for number in [0, 1, 2]:
    # Inside the code block
    print(7 * number)

# Inside the code block
    print("abc")
```

```
for number in [0, 1, 2]:
    # Inside the code block
    print(7 * number)
# Outside the code block
print("abc")
```

```
commline> python3 indentation1.py
0
abc
7
abc
```

```
commline> python3 indentation2.py
0
7
14
abc
```

- Indentation is very important in Python
- Code block ("bloc d'instructions")
 - A section of code which is grouped together.
 - Python groups code based on indentation

```
for number in [0, 1, 2]:
    # Inside the code block
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for number in [0, 1, 2]:
    # Inside the code block
    print(7 * number)
# Outside the code block
print("abc")
```

```
commline> python3 indentation1.py
0 abc
7 abc
14
```

```
commline> python3 indentation2.py
0
7
14
abc
```

- Indentation is very important in Python
- Code block ("bloc d'instructions")
 - A section of code which is grouped together.
 - Python groups code based on indentation
- Indentation: 4 spaces

```
for number in [0, 1, 2]:
    # Inside the code block
    print(7 * number)

# Inside the code block
    print("abc")
```

```
for number in [0, 1, 2]:
    # Inside the code block
    print(7 * number)

# Outside the code block
print("abc")
```

```
commline> python3 indentation1.py
0 abc
7 abc
14
```

```
commline> python3 indentation2.py
0
7
14
abc
```



Nested loop ("boucle imbriquée")

Nested loop: a loop inside a loop

```
for number1 in [4000, 1000]:
   for number2 in [20, 30]:
      print(number1 + number2)
```

```
commline> python3 forloopnested.py
4020
4030
1020
1030
```



Nested loop ("boucle imbriquée")

Nested loop: a loop inside a loop

```
for number1 in [4000, 1000]:
    for number 2 in [20, 30]:
        for number 3 in [6, 7]:
            print(number1 + number2 + number3)
```

```
commline> python3 forloopnested2.py
4026
4027
4036
4037
1026
1027
1036
1037
```



- Implement factorial: $f(n) = n! = 1 \cdot 2 \cdot \cdots \cdot (n-2) \cdot (n-1) \cdot n$
 - **1** Basic version (only for f(4), i.e. f(4) = 1 * 2 * 3 * 4 = 24)

```
# Algorithm: computes factorial = 4! = 1*2*3*4 = 24
factorial = 1
factorial = 2 * factorial # 2 <- 2*1
factorial = 3 * factorial # 6 <- 3*2
factorial = 4 * factorial # 24 <- 4*6
print(factorial) # Output
```

commline> python3 factorial0.py

24

- Implement factorial: $f(n) = n! = 1 \cdot 2 \cdot \cdots \cdot (n-2) \cdot (n-1) \cdot n$
 - **1** Basic version (only for f(4), i.e. f(4) = 1 * 2 * 3 * 4 = 24)
 - With for loop (only for f(4))

```
# Algorithm: computes factorial = 4! = 1*2*3*4 = 24
factorial = 1
for i in [2, 3, 4]:  # 2, 3, 4
    factorial = i * factorial # 2<-2*1, 6<-3*2, 24<-4*6

print(factorial) # Output</pre>
```



commline> python3 factorial1.py

24

- Implement factorial: $f(n) = n! = 1 \cdot 2 \cdot \cdots \cdot (n-2) \cdot (n-1) \cdot n$
 - **1** Basic version (only for f(4), i.e. f(4) = 1 * 2 * 3 * 4 = 24)
 - With for loop (only for f(4))
 - With range (only for f(4))

```
# Algorithm: computes factorial = 4! = 1*2*3*4 = 24
factorial = 1
for i in range(2, 4+1):  # 2, 3, 4
    factorial = i * factorial # 2<-2*1, 6<-3*2, 24<-4*6

print(factorial) # Output</pre>
```

@ 0 0 0 0 0 0 0 0

commline> python3 factorial1a.py

24

- Implement factorial: $f(n) = n! = 1 \cdot 2 \cdot \cdots \cdot (n-2) \cdot (n-1) \cdot n$
 - **1** Basic version (only for f(4), i.e. f(4) = 1 * 2 * 3 * 4 = 24)
 - With for loop (only for f(4))
 - With range (only for f(4))
 - With input (for f(n))

```
n = 4 # Input
# Algorithm: computes factorial = n! = 1*2*...*(n-2)*(n-1)*n
factorial = 1
for i in range(2, n+1):  # 2, 3, 4, ..., n-2, n-1, n
    factorial = i * factorial # 2=2*1, 6=3*2, 24=4*6, etc.

print(factorial) # Output
```

commline> python3 factorial2.py 24



- Implement factorial: $f(n) = n! = 1 \cdot 2 \cdot \cdots \cdot (n-2) \cdot (n-1) \cdot n$
 - **1** Basic version (only for f(4), i.e. f(4) = 1 * 2 * 3 * 4 = 24)
 - With for loop (only for f(4))
 - With range (only for f(4))
 - With input (for f(n))

```
n = 10 # Input
# Algorithm: computes factorial = n! = 1*2*...*(n-2)*(n-1)*n
factorial = 1
for i in range(2, n+1):  # 2, 3, 4, ..., n-2, n-1, n
    factorial = i * factorial # 2=2*1, 6=3*2, 24=4*6, etc.

print(factorial) # Output
```

commline> python3 factorial2a.py 3628800



Conditional execution ("alternatives")

- if statement ("test si")
 - execute intructions only if a certain condition holds

```
a = 3
b = 4
if (a < b): # Condition (expression yielding boolean)</pre>
    print("a is smaller than b")
if (b <= a): # Condition (expression yielding boolean)</pre>
    print("b is smaller than or equal to a")
```

```
commline> python3 ifstatement.py
a is smaller than b
```



Conditional execution ("alternatives")

- if statement ("test si")
 - execute intructions only if a certain condition holds
- if-then-else statement ("test si sinon"): for convencience

```
a = 3
b = 4
if (a < b): # Condition (expression yielding boolean)</pre>
    print("a is smaller than b")
else:
          # If condition above doesn't hold
    print("b is smaller than or equal to a")
```

```
commline> python3 ifthenelsestatement.py
a is smaller than b
```



Conditional execution ("alternatives")

- if statement ("test si")
 - execute intructions only if a certain condition holds
- if-then-else statement ("test si sinon"): for convencience
- elif: combines else and if: for convencience

```
a = 3
b = 4
if (a < b): # Condition (expression yielding boolean)
    print("a is smaller than b")
elif (a > b): # Condition (expression yielding boolean)
    print("a is larger than b")
else: # If conditions above do not hold
    print("a is equal to b")
```

```
commline> python3 ifthenelifelsestatement.py
a is smaller than b
```



Control Flow: while loop ("boucle tant que")

- Combines a loop with a condition
 - useful when you don't know number of iterations in advance

```
# Print(the first multiple of 7)
# that is larger than 10000
number = 0
while (number <= 10000):
  number = number + 7
print(number)
```

```
commline> python3 whileloop.py
10003
```



Outline

- Algorithms
- Programming
- Cours IN101
- Python Basics
 - Python Interpreter
 - Variables
 - Operators
 - Control flow
 - Ancient algorithms still used today
- 5 TD



- Specification: Greatest common divisor ("Plus grand commun diviseur")
 - Divisors of 12: 1, 2, 3, 4, 6, 12
 - Divisors of 16: 1, 2, 4, 8, 16
 - Greatest common divisor of 12 and 16: 4



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 - Divisors of 12: 1, 2, 3, 4, 6, 12
 - Divisors of 16: 1, 2, 4, 8, 16
 - Greatest common divisor of 12 and 16: 4
- Algorithm: Euclid's algorithm in English
 - Starting with a pair of positive integers, form a new pair consisting of the smaller number and the
 difference between the larger number and the smaller number. This process repeats until the
 numbers in the new pair are equal to each other; that value is the greatest common divisor of the
 original pair. (taken from Wikipedia)



Euclid's algorithm ($\approx 300 \text{ BC}$)

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- Programming: Euclid's algorithm in Python

```
a = 12 \# Input
```



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- Programming: Euclid's algorithm in Python

```
a = 12 # Input
b = 16 # Input

if (a > b):
    a = a - b # 'a' is the largest number
else:
    b = b - a # 'b' is the largest number
```



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```
a = 12 # Input
b = 16 # Input

while (???):  # continue until...
   if (a > b):
        a = a - b # 'a' is the largest number
   else:
        b = b - a # 'b' is the largest number
```



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- Programming: Euclid's algorithm in Python

```
a = 12 # Input
b = 16 # Input

while (a != b): # continue until 'a' and 'b' are equal
   if (a > b):
        a = a - b # 'a' is the largest number
   else:
        b = b - a # 'b' is the largest number
```



Euclid's algorithm ($\approx 300 \text{ BC}$)

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        a = a - b # 'a' is the largest number
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gcd = a
print(gcd) # Output
```

Euclid's algorithm ($\approx 300 \text{ BC}$)

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- Why is a > 2 millenia old algorithm still important today?
 - Used in security protocols (e.g. in the RSA algorithm)
 - Any secure communication (e.g. https://) will call this algorithm many times



Sieve of Eratosthenes (≈ 200 BC)

- Prime number ("nombre premier")
 - natural number {1,2,3,...}
 - greater than 1
 - only 2 positive divisors: 1 and itself
- Requested algorithm
 - Input: number n
 - Output: all prime numbers ≤ n



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Design an algorithm for this with your neighbor(s)!



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 - Input: number n
 - Output: all prime numbers ≤ n

Design an algorithm for this with your neighbor(s)!

Sieve of Eratosthenes

- Eratosthenes of Cyrene, 276 BC 195 BC
- · Found one of the most efficient algorithms
- Explanation will have to wait until CM3...





- Requested algorithm
 - Input: n, the product of two unknown primes $n = a \cdot b$
 - Output: a and b



- Requested algorithm
 - Input: n, the product of two unknown primes n = a ⋅ b
 - Output: a and b
- Finding a slow algorithm is straightforward (TD2)
 - Ompute all primes up to n-2
 - · Using the algorithm you just made
 - · Or the Sieve of Eratosthenes
 - Multiply combinations of primes until you get n



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- Finding a fast algorithm is really difficult



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 - · Or the Sieve of Eratosthenes
 - Multiply combinations of primes until you get n
- Finding a fast algorithm is really difficult
 - if you find a fast algorithm, I will pay you 1.000.000EUR for it.



Summary of this CM

- Algorithm
 - · a recipe with input, instructions, and output
 - a set of rules that precisely defines a sequence of operations.
- Programming
 - implement algorithms in a (formal) language that can be written by a human, and executed by a computer
- Python
 - programming language, easy to learn, fun, Monty Python
 - executing instructions in a script: Python interpreter
- Python language
 - variables: names with values
 - types of values: numbers, lists, strings, booleans
 - operators: combining values and variables
 - · control flow: for, if, while



Aims of the upcoming TD

- · Write your first Python program, calling the interpreter
- · Design your first algorithm
- · Program your first algorithms
- Create a clean, comfortable programming environment
 - · Choose an editor you are proficient in
- Learn to find solutions yourself, with help from
 - the slides
 - the Python documentation: https://docs.python.org/3/
 - your favourite search engine
 - the books that are provided as PDFs



Part I: Basics

CM1 variables, control flow CM2 functions and modules

CM3 lists, arrays, dictionaries

factorial(6), import math

 $[2, 3, 1] \rightarrow [1, 2, 3]$

a=1, for/if/while

[2, 3, 1]

Part II: Data Structures (Built-in)

Part III: Search and Sort

CM4 searching/sorting

CM5 Exam 1

Part IV: Linked Data Structures

CM6 objects/classes

CM6 objects/classes
CM7 linked lists

CM8 trees

Evam

CM9 Exam 2

 $a' \rightarrow e' \rightarrow b' \rightarrow x$

circle object = Circle(0,1,3)

W

Have fun programming your first algorithms in the first TD!

