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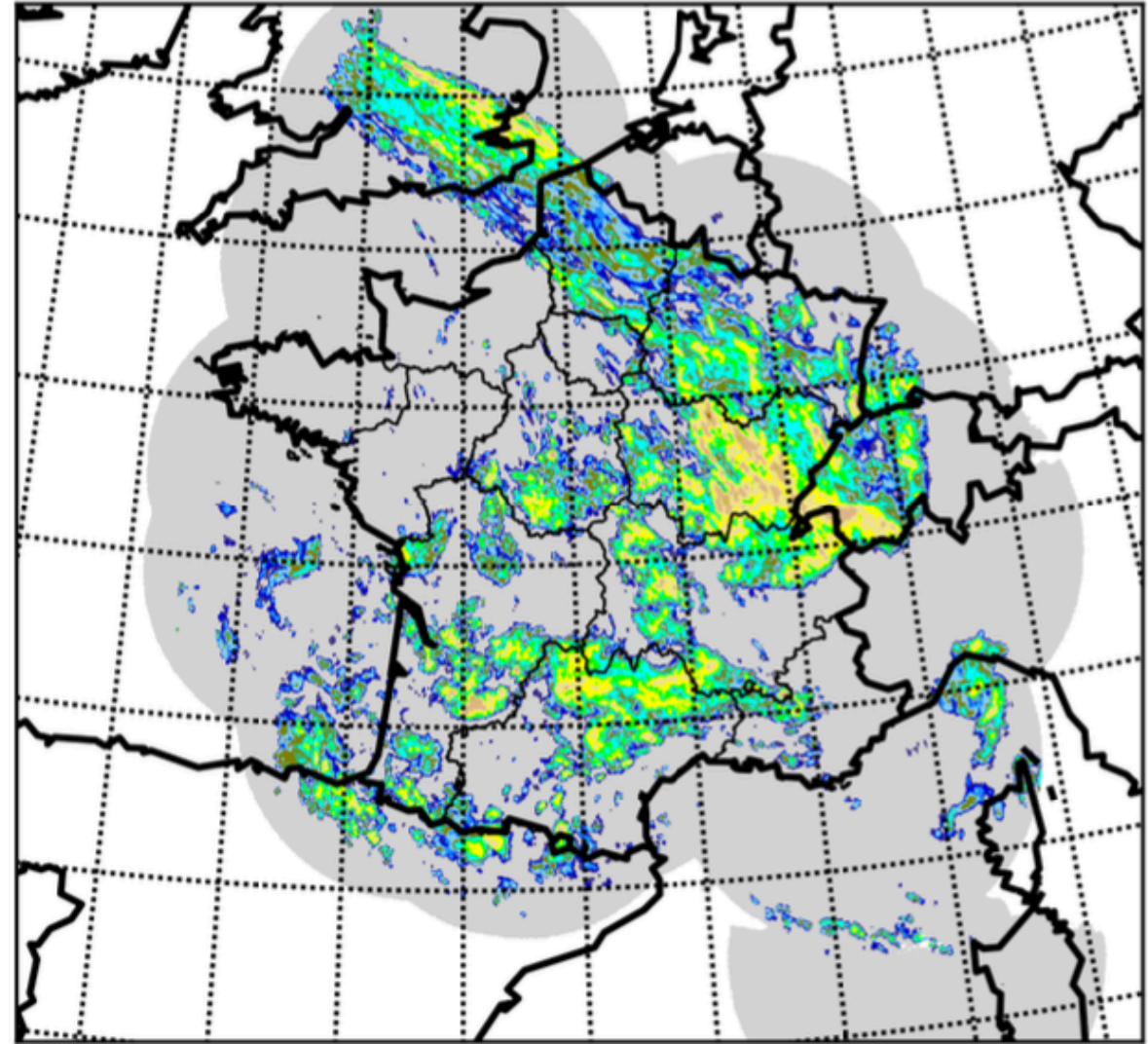
# AI/DL and Nowcasting of Extremely Variable Fields

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Polytechnique de Paris



USP-PPI workshop  
111 March 2025



## • Hydrology Meteorology and Complexity

- geophysics/environment to be investigated as a complex system
  - HM&Comoto: **strong variability/heterogeneity** of natural and man-made environments **over a wide range of scales**
    - not only applications: this inspires/requires new complexity concepts and techniques
      - cascades
      - multifractals
      - complex networks
      - scaling anisotropy
    - more and more data of higher quality and resolution

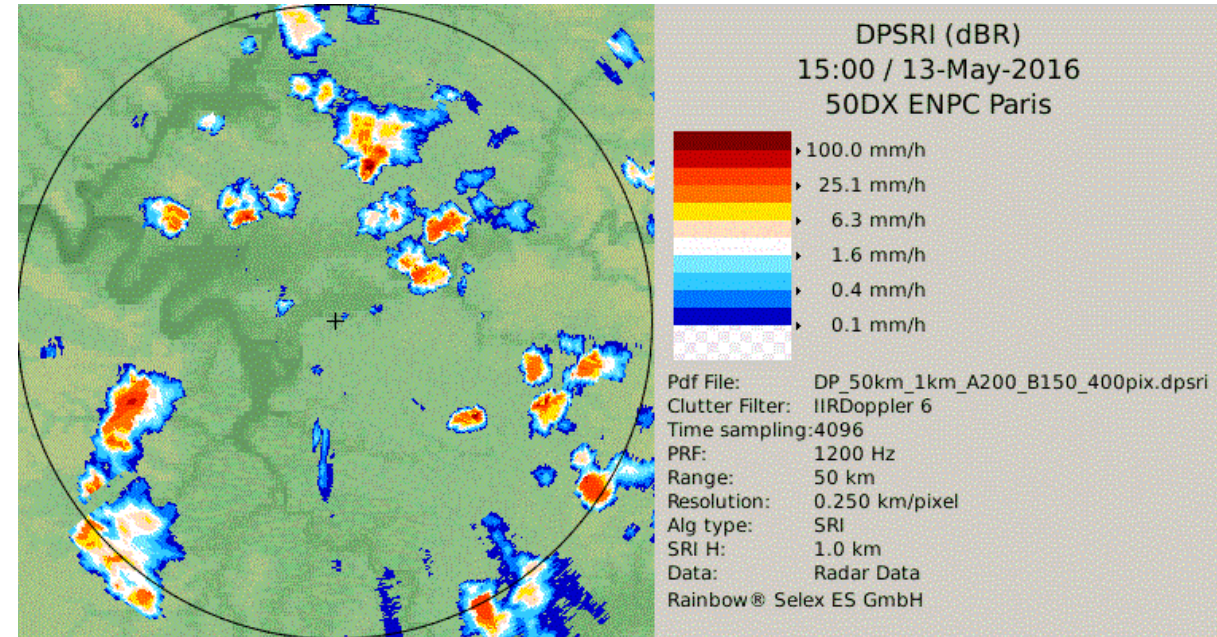


# Millenium problem of turbulence !

explO ratorium®



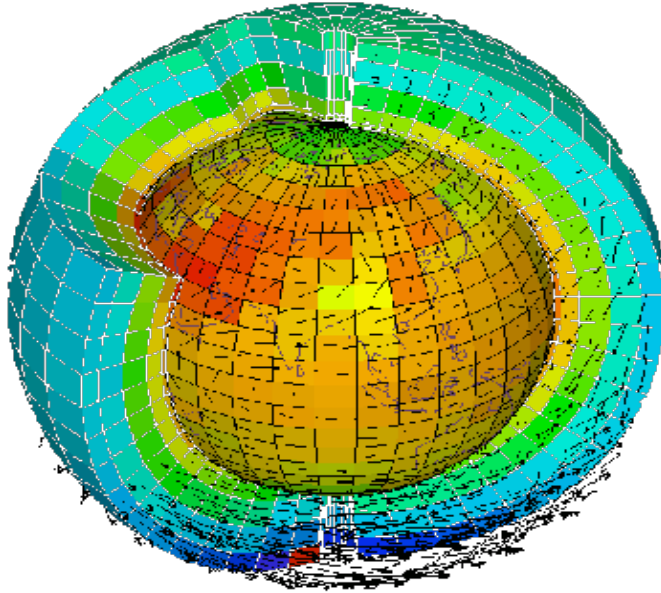
**Art piece 'Windswept'** (Ch. Sowers, 2012): 612 freely rotating wind direction indicators to help a large public to understand the complexity of environment near the Earth surface



Polarimetric radar observations of heavy rainfalls over Paris region during 2016 spring (100 m resolution):

- **heaviest rain cells** are much smaller than **moderate ones**
- **complex dynamics** of their aggregation into a large front

# How many scales and voxels?



Computing brute force  
sufficient?

It requires  $N$  cubes of  $\text{mm}^3$   
to reach the ***viscous scale***  
( $\approx 1\text{mm}$ ):

$$N \approx 10^7 (10^{10})^2 = 10^{27} \gg$$

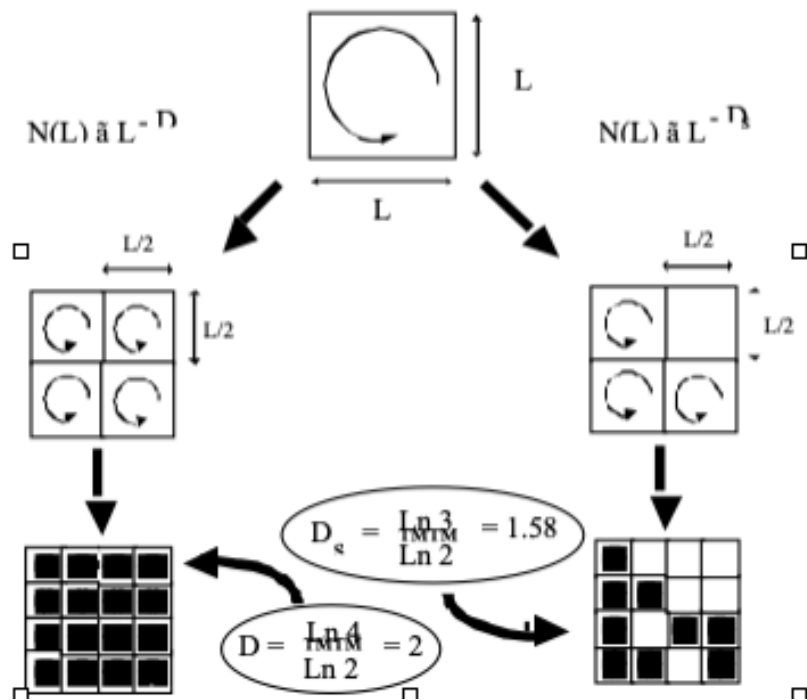
$$N_A = 10^{23}$$

whereas  $N_{\text{effective}} \approx 10^7 - 10^6$

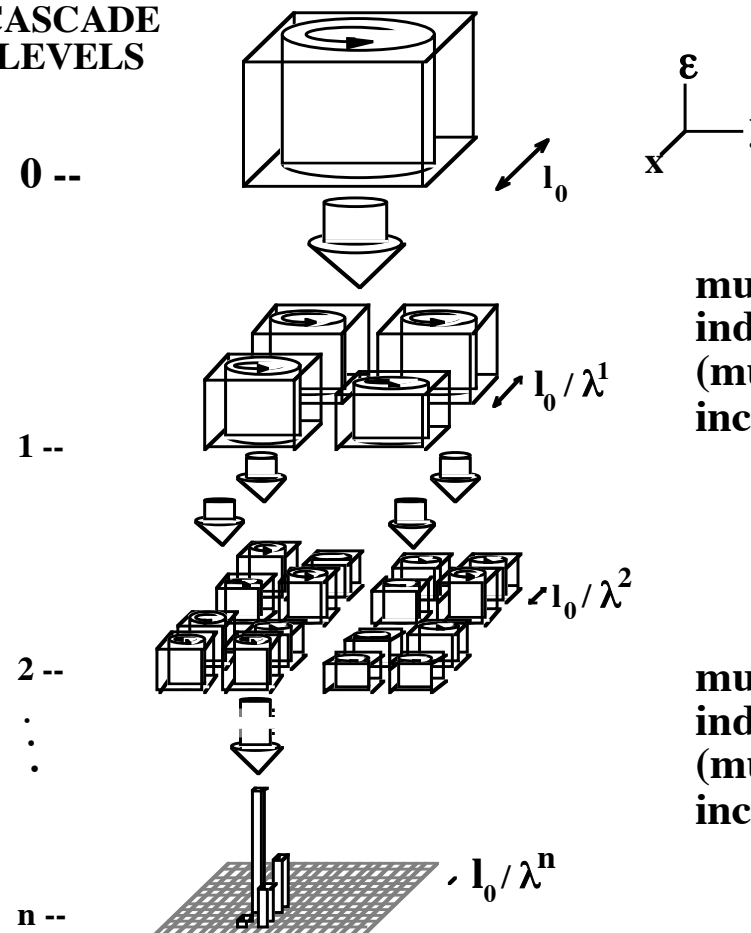
$\implies$  statistics or stochastics ?

# Phenomenology: multiplicative cascades

- Richardson's quatrain (1922) :  
*Big whirls have little whirls that feed on their velocity and little whirls have lesser whirls and so on to viscosity... in the molecular sense.*
- discrete multiplicative cascade processes (Yaglom 1966, Mandelbrot 1974...)
- From dead/alive alternative ( $\beta$ -model) to weak/strong infinite hierarchy of intensities
- supported by an infinite hierarchy of fractals,
- i.e. these fields are in general **MULTIFRACTAL**
- however, multiplicative processes are not indispensable !



## CASCADE LEVELS

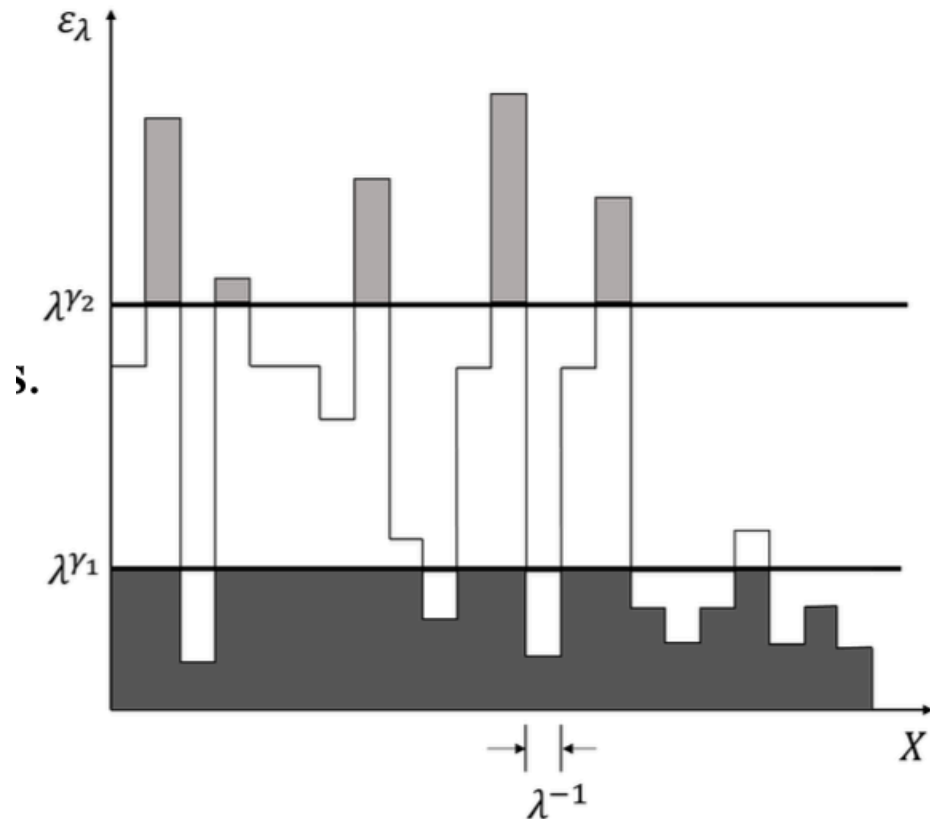


**multiplication by 4  
independent random  
(multiplicative)  
increments**

**multiplication by 16  
independent random  
(multiplicative)  
increments**



# Universal Multifractals (UM)



A schematic illustration of a multifractal field analysed over a scale ratio  $\lambda$ , with two scaling thresholds,  $\lambda^{\gamma_1}$  and  $\lambda^{\gamma_2}$ , corresponding to two orders of singularity:  $\gamma_2 > \gamma_1$ .

- **Multifractals:** increasing **variability clusters** on smaller and smaller space-time fractions, in fact **fractal subsets**
  - => multi-scaling:  $\langle \varepsilon_\lambda^q \rangle \approx \lambda^{K(q)}$ , the scaling function  $K(q)$  is nonlinear for a wide range of resolutions  $\lambda = L/\ell$
- **Universal Multifractals (UM):** stable and attractive multifractal processes:  $K(q) = \frac{C_1}{\alpha - 1}(q^\alpha - q)$ 
  - $0 < C_1$ : **mean intermittency**, also the singularity of the mean field. The field is homogeneous for  $C_1 = 0$
  - $0 \leq \alpha \leq 2$ : **multifractality index**, measures the increase of the intermittency with deviation from the mean. The field is monofractal for  $\alpha = 0$ , lognormal for  $\alpha = 2$ .
- **Non-conservative fields:**  $\varphi_\lambda \stackrel{d}{=} \varepsilon_\lambda \lambda^{-H}$  introduces the **non-conservative parameter  $H$** , e.g. order of fractional integration/derivation.

# Varenna summer school (1983)

Homogeneous  
or monofractal

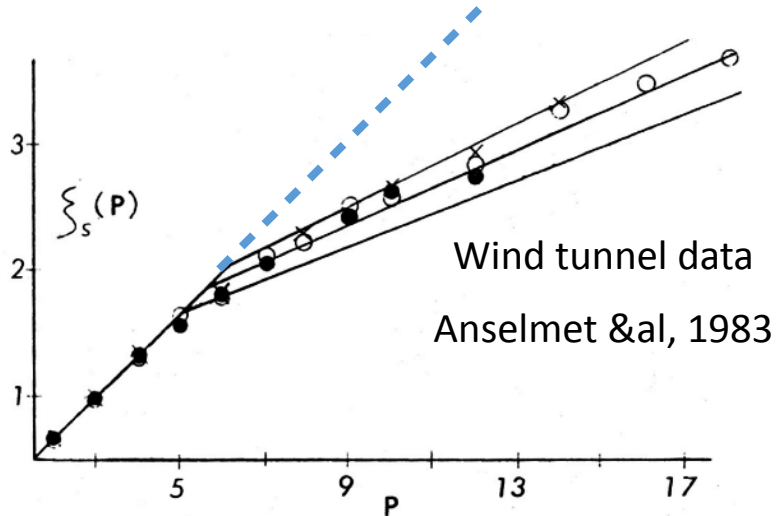


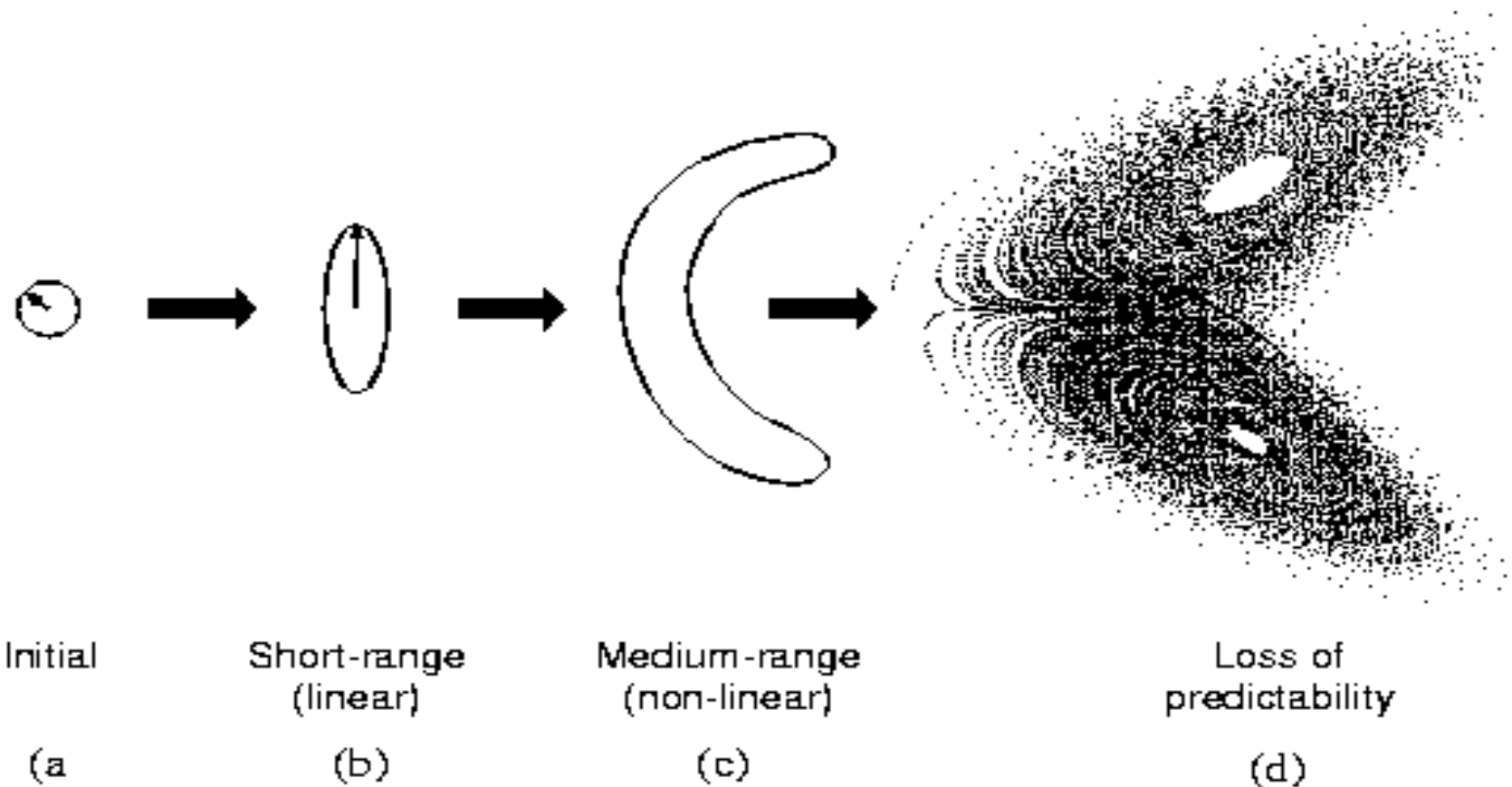
Fig.1 from S+L (1984)

- primary version of the multifractal formalism of Parisi and Frisch (1985) presented at “Turbulence and Predictability in Geophysical Fluid Dynamics” organised by M. Ghil, R. Benzi et G. Parisi
- clustering of higher activity on smaller spacetime fractions
- but: **“Still the multifractal model appears to be somewhat more restrictive than Mandelbrot’s weighted-curdling model which does include the lognormal case”**.
- the conference proceedings (1985) refers to S+L (1984)):
  - a small perturbation of the  $\beta$ -model is no longer limited to a unique dimension ( $\alpha$ -model)
  - the divergence of higher order moments is rather generic in cascade models
  - the later introduces spurious scaling, an analytical approximation depending on a unique scaling exponent  $H$  and the critical order  $\alpha$  was proposed:
  - it was shown to fit the [experimental points from Anselmet et al. \(1983\)](#), see fig. 1 with:

$$\xi(p) = pH + \theta(p - \alpha)(1 - p/\alpha)$$

$$H = 1/3, \alpha = 5, 5.5, 6$$

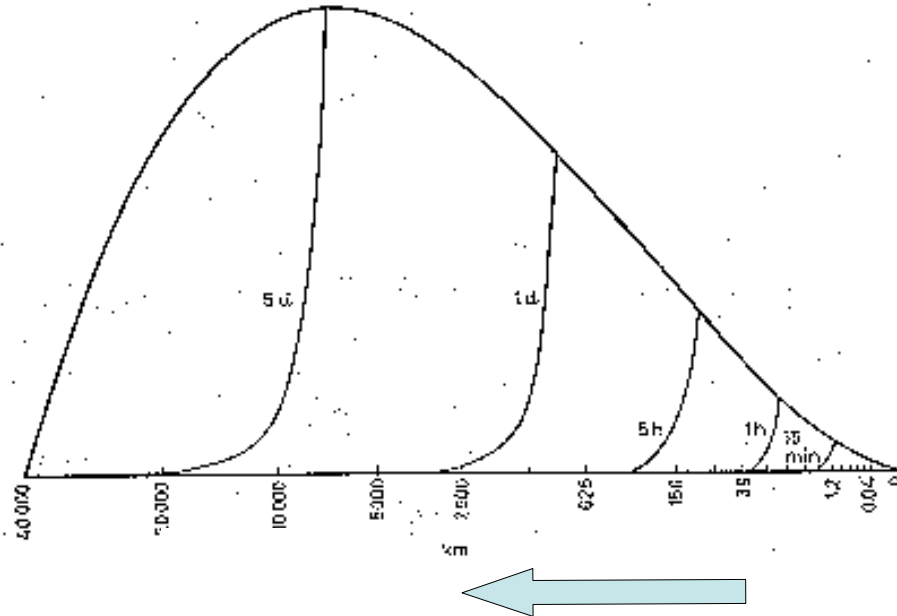
# Butterfly effect and ensemble predictions



**Scheme of the evolution of the empirical pdf evolution of an Ensemble Prediction System (EPS), according to Palmer, 1999:** from the phase space region occupied by the initial ensemble (a), to (b) linear growth phase, to (c) nonlinear growth phase, to (d) loss of predictability



# Spectral analysis of space-time predictability



Flux from correlated  $e^c$  to decorrelated energy  $e^\Delta$

Similar results with turbulence phenomenology:

$$\ell_c = 1/k_c \approx t^{3/2}$$

Lorenz (1969)

Leith and Kraichnan(1972)

Metais and Lesieur (1986)

$$e^c(\underline{x}, t) = \underline{u}^2(\underline{x}, t) \cdot \underline{u}^1(\underline{x}, t)$$

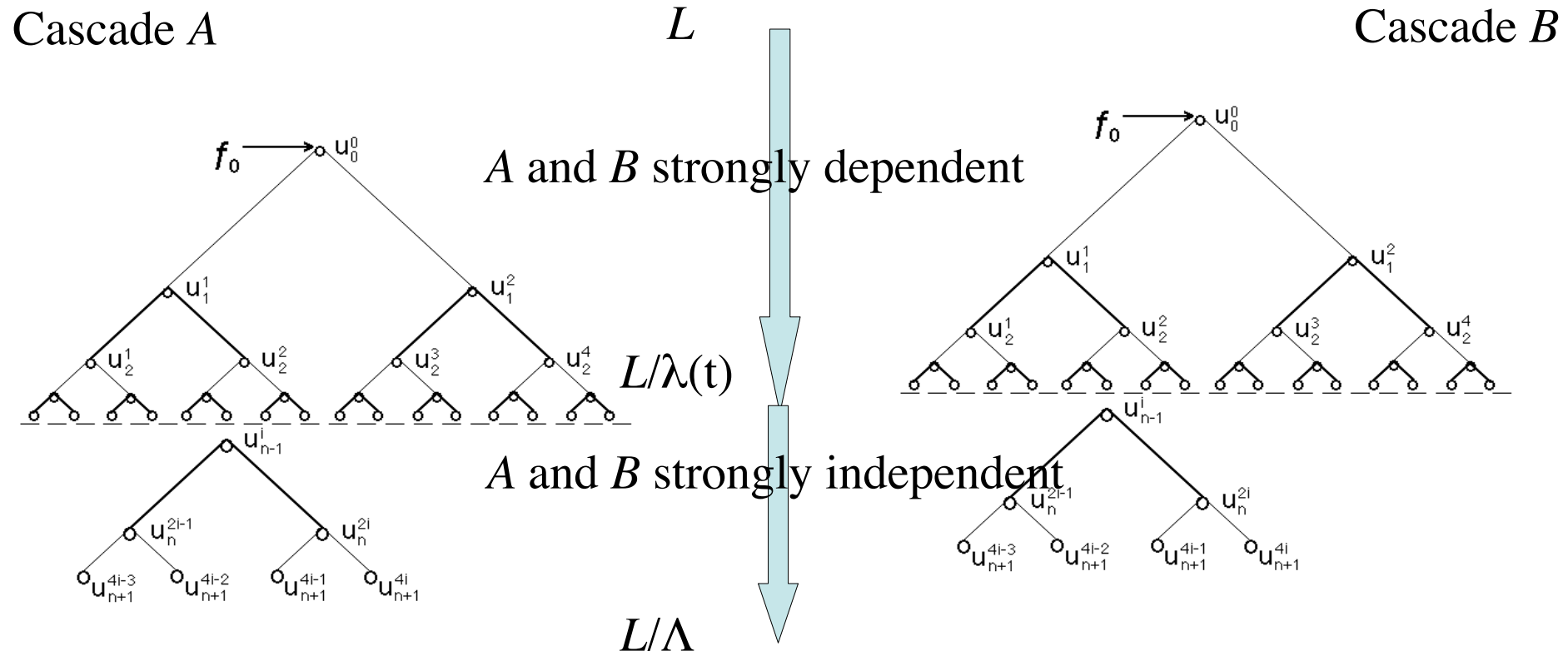
$$e^\Delta(\underline{x}, t) = \frac{1}{2} \left( \underline{u}^2(\underline{x}, t) - \underline{u}^1(\underline{x}, t) \right)^2$$

$$\ell \approx \bar{\varepsilon}^{1/2} t^{3/2}; \quad \bar{\varepsilon} \approx 10^{-3} m^2 s^{-3}, \quad \eta = 10^{-3} m$$

# Multifractal Predictability

Rough idea:

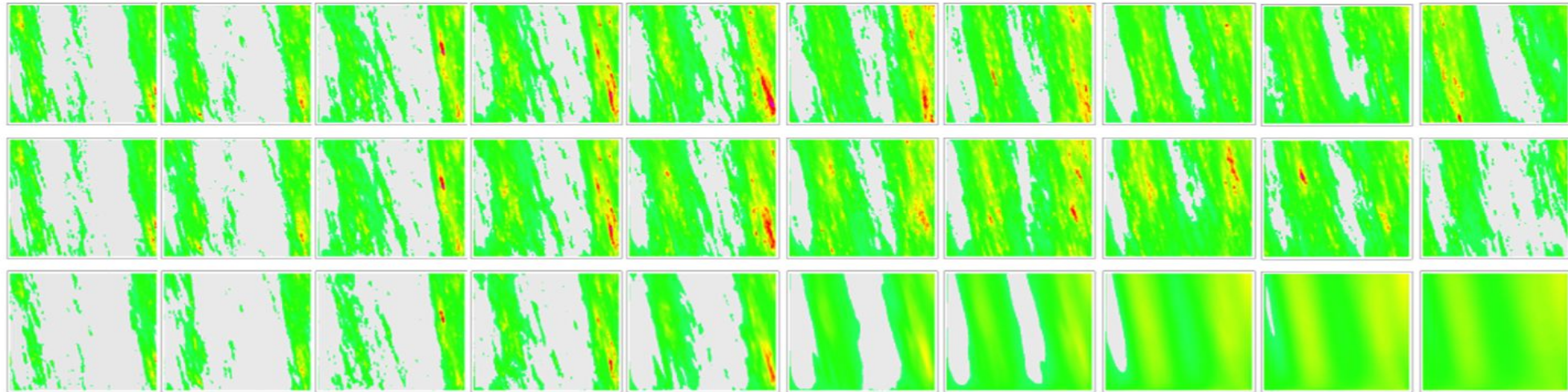
- i) relaxation of (common) past structures  $\implies$  flux of the past
- ii) (new) independent structures  $\implies$  flux of the future



# Multifractal Predictability

Rain simulation ( $\alpha=1.5$ ,  $C_1=0.2$ ,  $H=0.1$  on log scale. Realizations A, B are identical until  $t=0$ , then they diverge.

Top: Realization A. Middle: Realization B. Bottom, forecast



- **Power law divergence** between the realizations A and B,  
=> **irrelevance** of the **finite dimensional ‘LE + MET’ scenario !**
- **Drastic loss of variability of forecast C** with deterministic sub-grid modeling (based on the conservation of the flux) => **‘baby theorem’**: **stochastic sub-grid modeling** does much better than deterministic one!

# Rainfall time series prediction: VMD-RNN

**Step1: Divide the original rainfall time series into a training set and a non-training set.**

**Step2: Decompose the training set into  $K$  sub-sequences using VMD.**

**Step3: Sequentially append the non-training data to the training set to generate new appended sequences and repeat decompose each append sequence into  $K$  sets of appended sub-sequences.**

**Step4: Extract the last sample of each set of appended sub-sequences as a non-training sample.**

**Step5: For each sub-sequences, train four variant RNN models and tune hyperparameters to find an ideal predicting model with optimal parameters.**

**Step6: For each sub-sequences, input testing samples into the correspond predicting models, and obtain individual predicted results  $y_i(t)$ .**

**Step7: Aggregate the predicting results of each sub-sequences to generate the final predicted result  $y(t) = \sum_{i=k}^K y_i(t)$ .**

**Step8: Use the framework of UM to analyze the predicted and actual time series in the testing samples.**

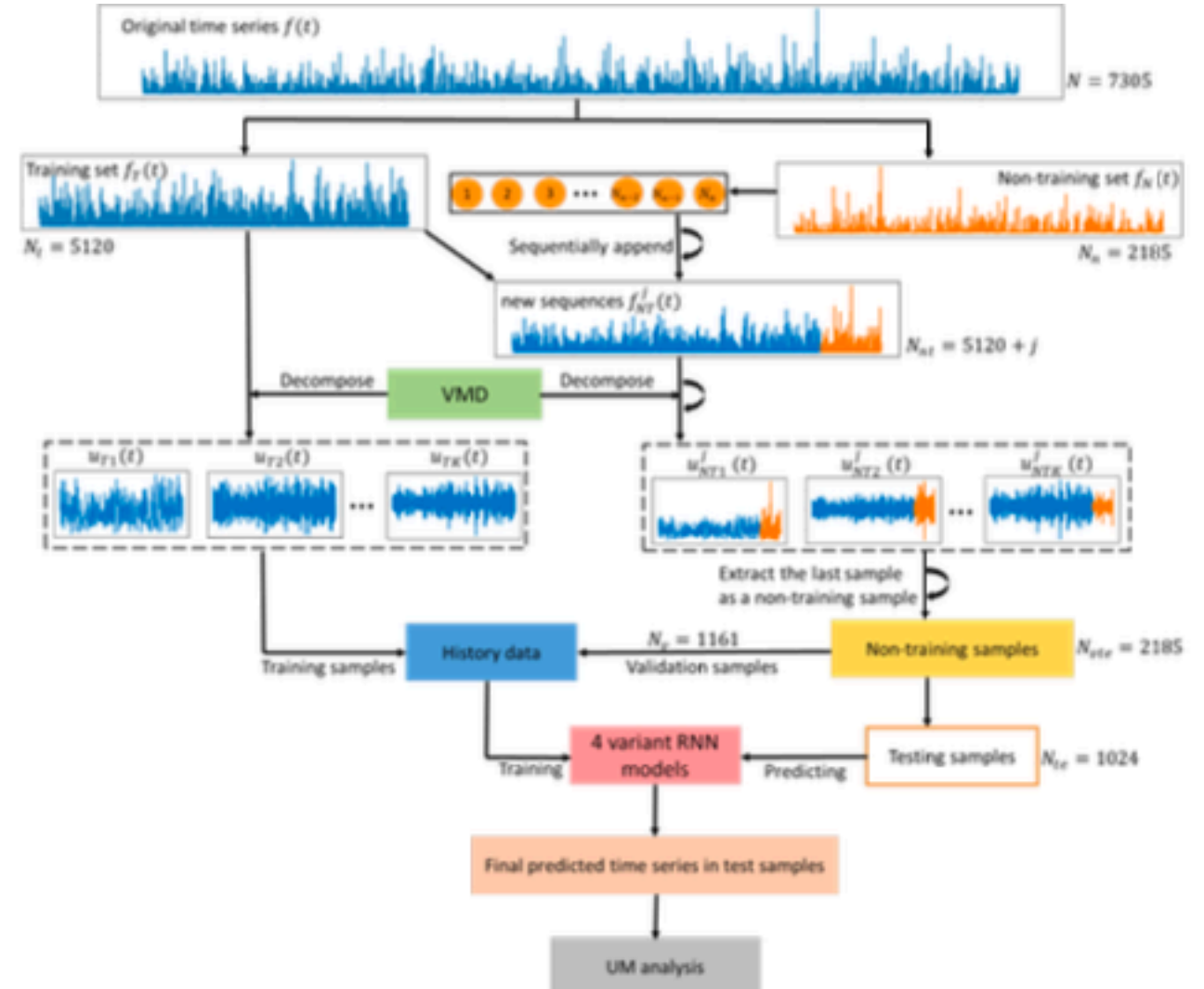


Figure 22: The process of the VMD-RNN model (Zhou et al, 2022)

# Rainfall time series prediction: VMD-RNN

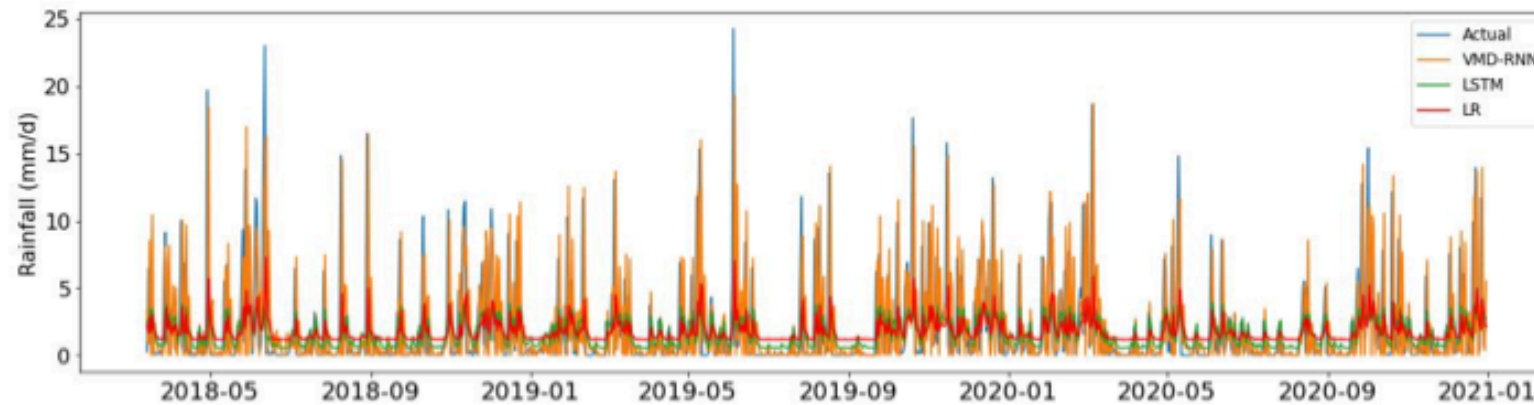


Figure 25: Predicted and actual daily time series in the testing set

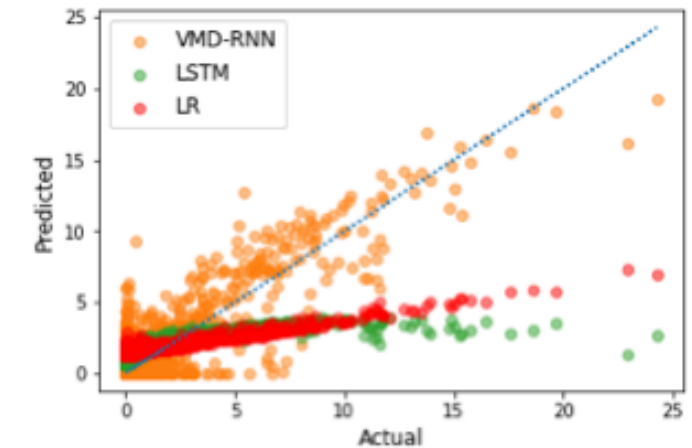


Figure 26: The comparison between predicted and actual daily rainfall values

Table 4: Prediction errors for daily time series in the testing set

	MAE	RMSE	MAPE
VMD-RNN	0.726	0.852	9.853
LSTM	6.825	2.612	10.475
LR	9.239	3.040	18.923

- VMD-RNN model has better performance in predicting high and low values, compared with the pure LSTM and linear regression
- VMD-RNN model has lowest prediction errors in MAE, RMSE, MAPE

# Rainfall time series prediction: VMD-RNN

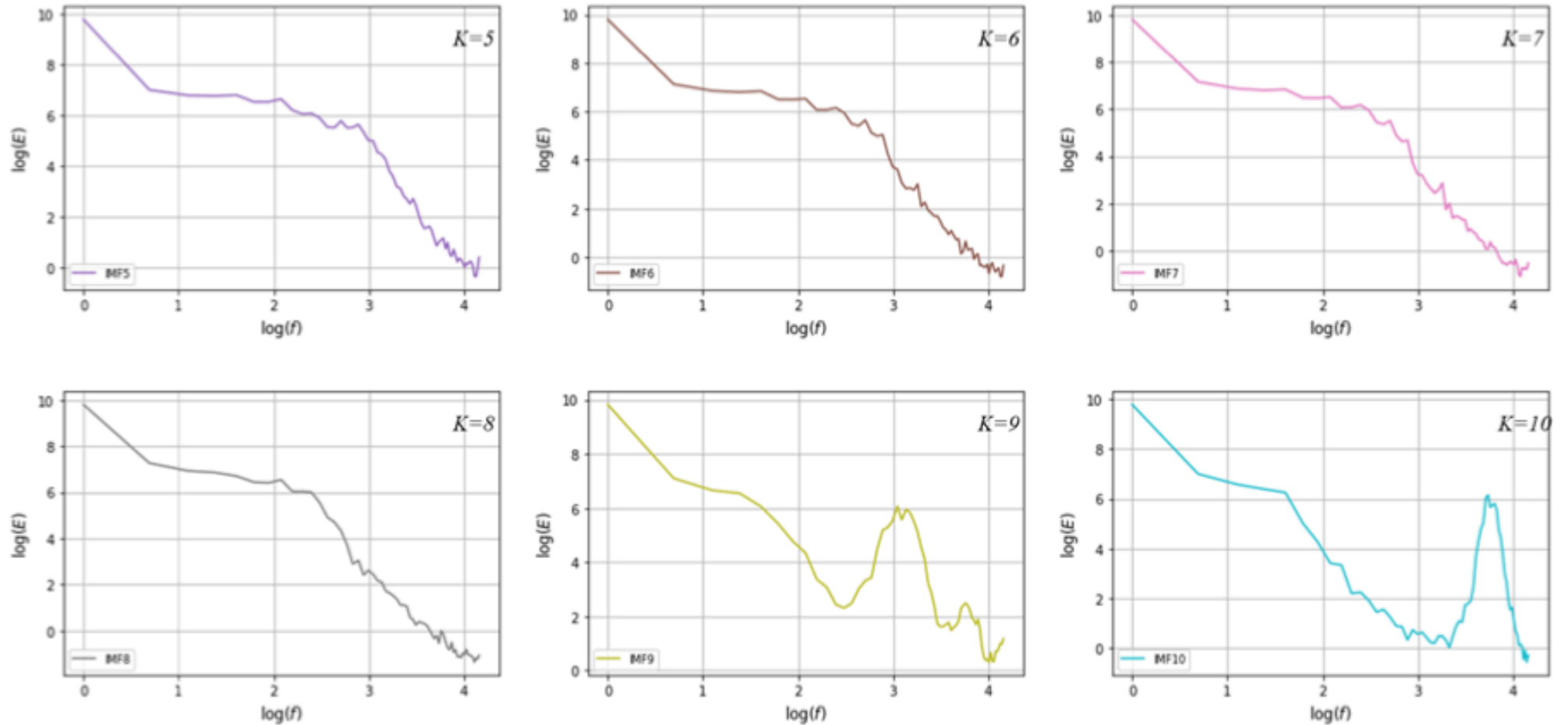


Figure 23: PSD of the corresponding last sub-sequence when  $K$  from 5 to 10

# Methodologies: multifractal time series analyses

## ➤ Trace Moment (TM):

- i. Calculate the empirical statistical moment  $\langle \varepsilon_\lambda^q \rangle$
- ii. Plot the logarithm of  $\langle \varepsilon_\lambda^q \rangle$  versus the logarithm of  $\lambda$
- iii. Perform linear regression to obtain  $K(q)$
- iv.  $K'(1) = C_1$  and  $K''(1) = \alpha C_1$

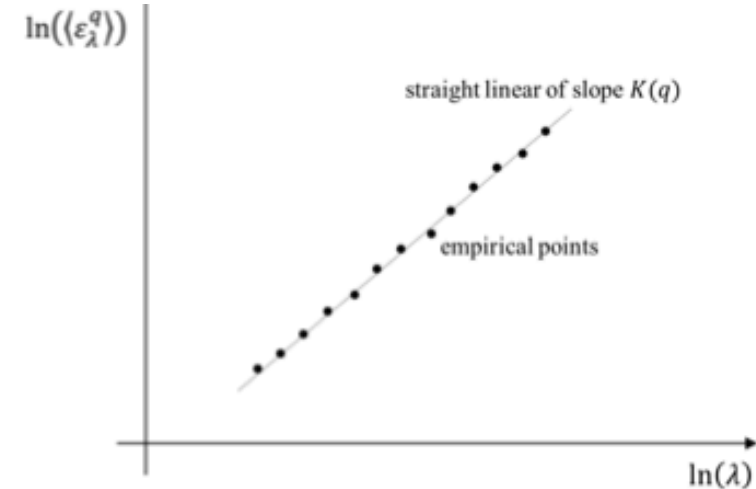


Figure 17: Illustration of the Trace Moment technique (Image source: Gires, 2012)

## ➤ Double Trace Moment (DTM):

- i.  $\varepsilon_\lambda^{(\eta)}$  is renormalized by upscaling the  $\eta$ -power of the field at maximum resolution
- ii.  $\langle \varepsilon_\lambda^{(\eta)q} \rangle \approx \lambda^{K(q,\eta)}$ ,  $K(q,\eta) = \eta^\alpha K(q)$
- iii.  $C_1$  and  $\alpha$  are obtained by the slope and intercept of the linear portion of the log-log plot of  $K(q,\eta)$  vs  $\eta$

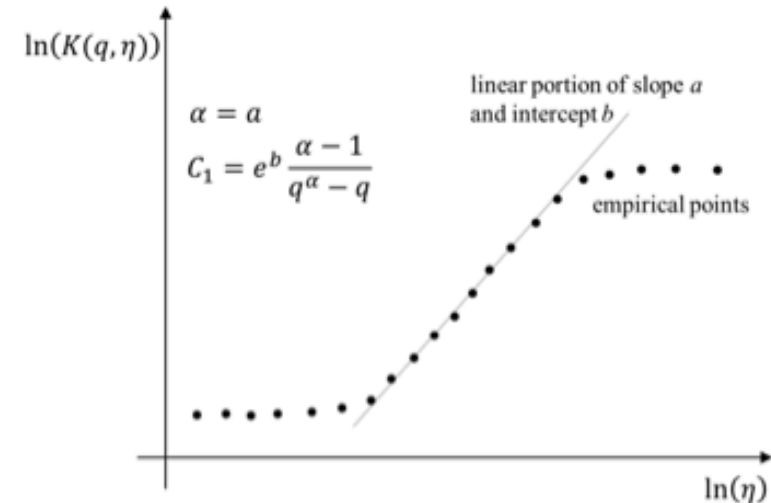
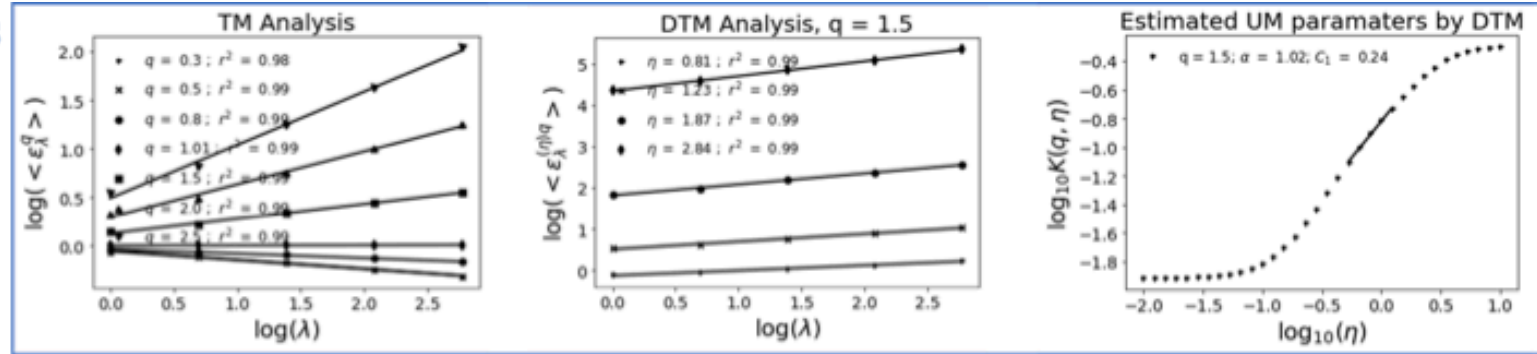


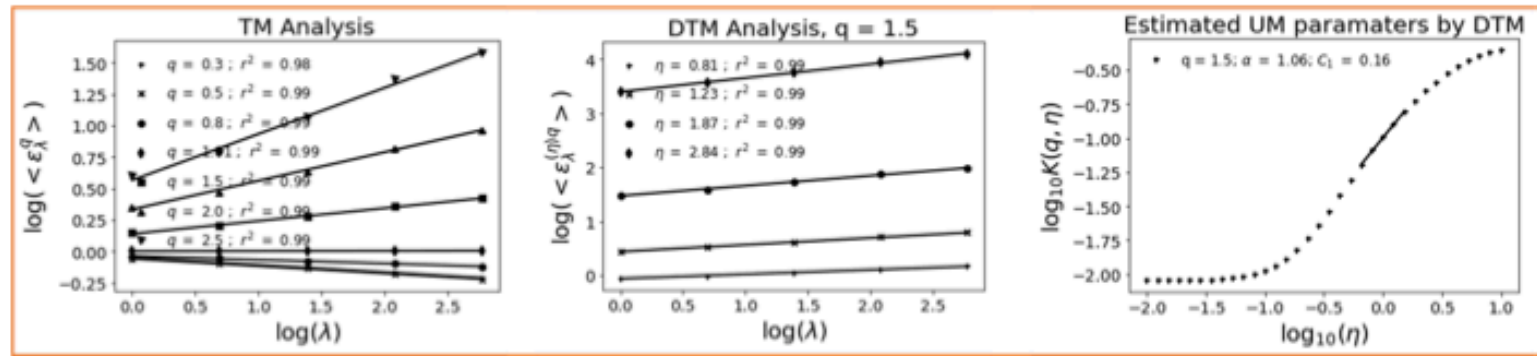
Figure 18: Illustration of the Double Trace Moment technique (Image source: Gires, 2012)

# Rainfall time series prediction: VMD-RNN

actual time series



predicted time series by  
VMD-RNN



predicted time series by LSTM  
without decomposition

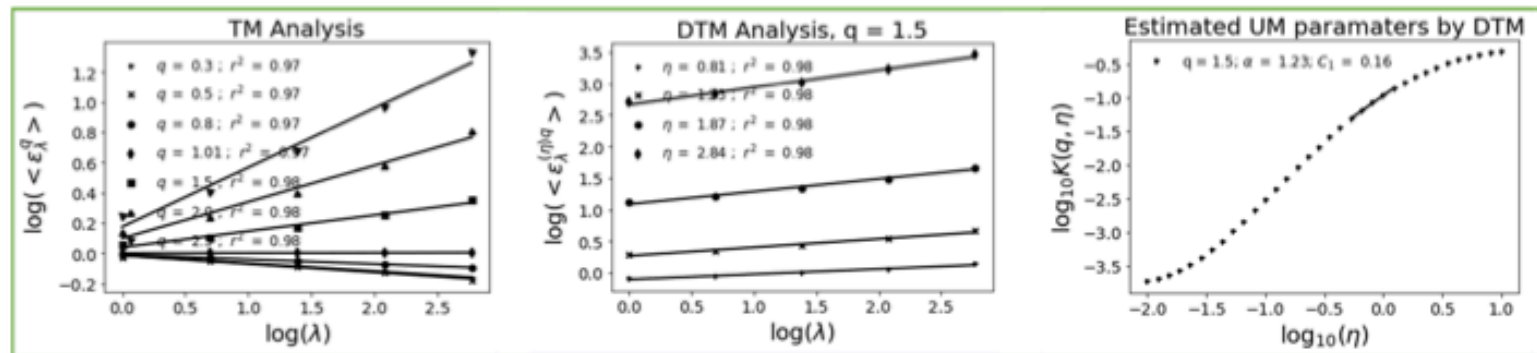
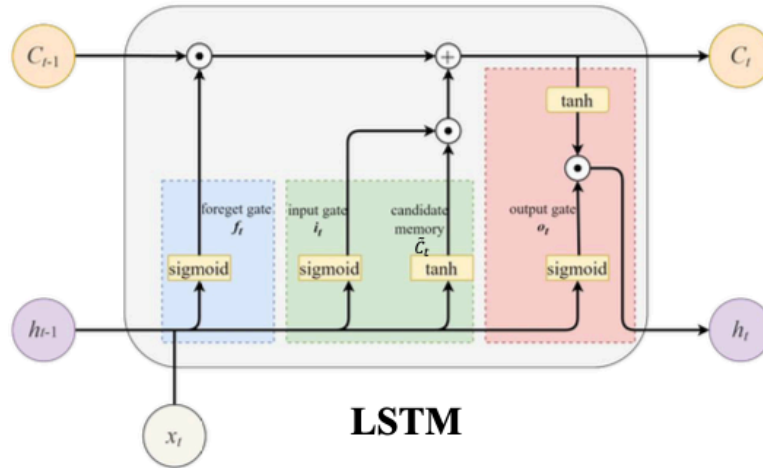
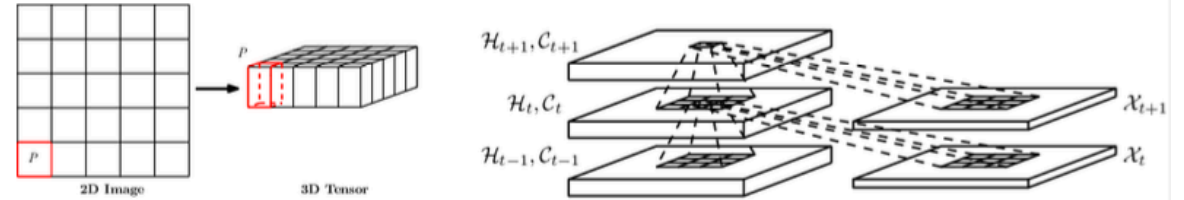


Figure 27: UM results for daily time series in the testing set



# Methodologies: LSTM and ConvLSTM

spatio-temporal prediction:



**LSTM**

$$f_t = \sigma(W_{xf} x_t + W_{hf} h_{t-1} + b_f)$$

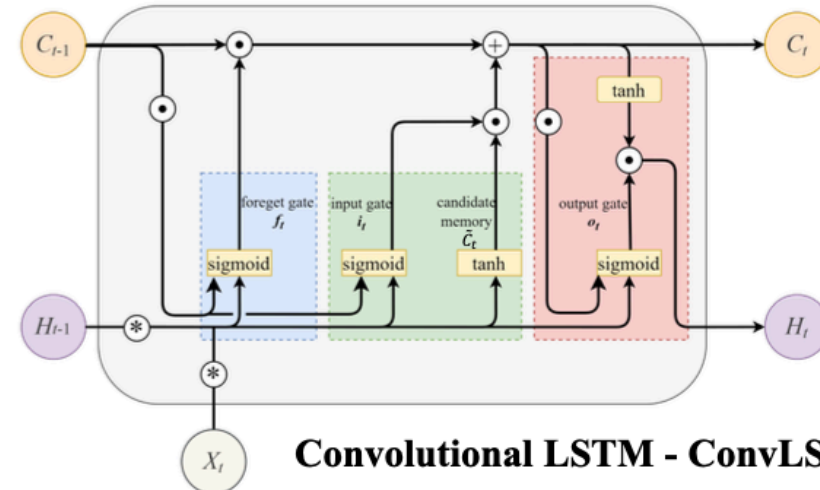
$$i_t = \sigma(W_{xi} x_t + W_{hi} h_{t-1} + b_i)$$

$$\tilde{C}_t = \tanh(W_{xc} x_t + W_{hc} h_{t-1} + b_c)$$

$$C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$$

$$o_t = \sigma(W_{xo} x_t + W_{ho} h_{t-1} + b_o)$$

$$h_t = o_t \odot \tanh(C_t)$$



**Convolutional LSTM - ConvLSTM**

$$f_t = \sigma(W_{xf} * x_t + W_{hf} * \mathcal{H}_{t-1} + W_{cf} \odot C_{t-1} + b_f)$$

$$i_t = \sigma(W_{xi} * x_t + W_{hi} * \mathcal{H}_{t-1} + W_{ci} \odot C_{t-1} + b_i)$$

$$\tilde{C}_t = \tanh(W_{xc} * x_t + W_{hc} * \mathcal{H}_{t-1} + b_c)$$

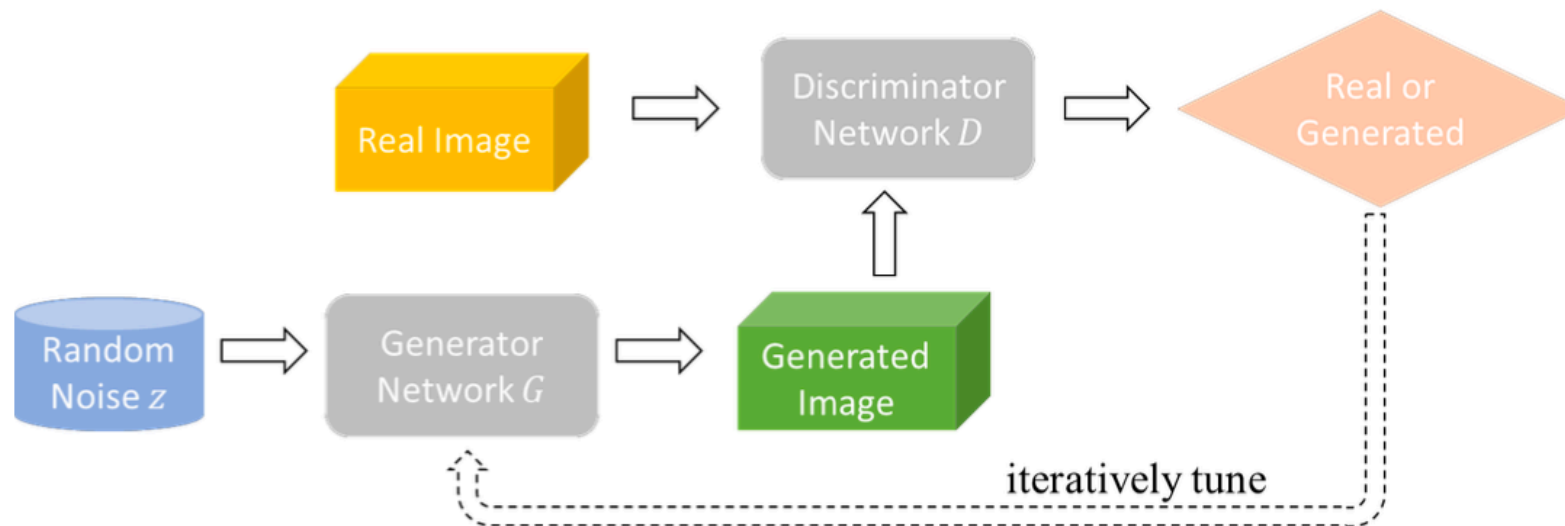
$$C_t = f_t \odot C_{t-1} + i_t \odot \tilde{C}_t$$

$$o_t = \sigma(W_{xo} * x_t + W_{ho} * \mathcal{H}_{t-1} + W_{co} \odot C_t + b_o)$$

$$\mathcal{H}_t = o_t \odot \tanh(C_t)$$

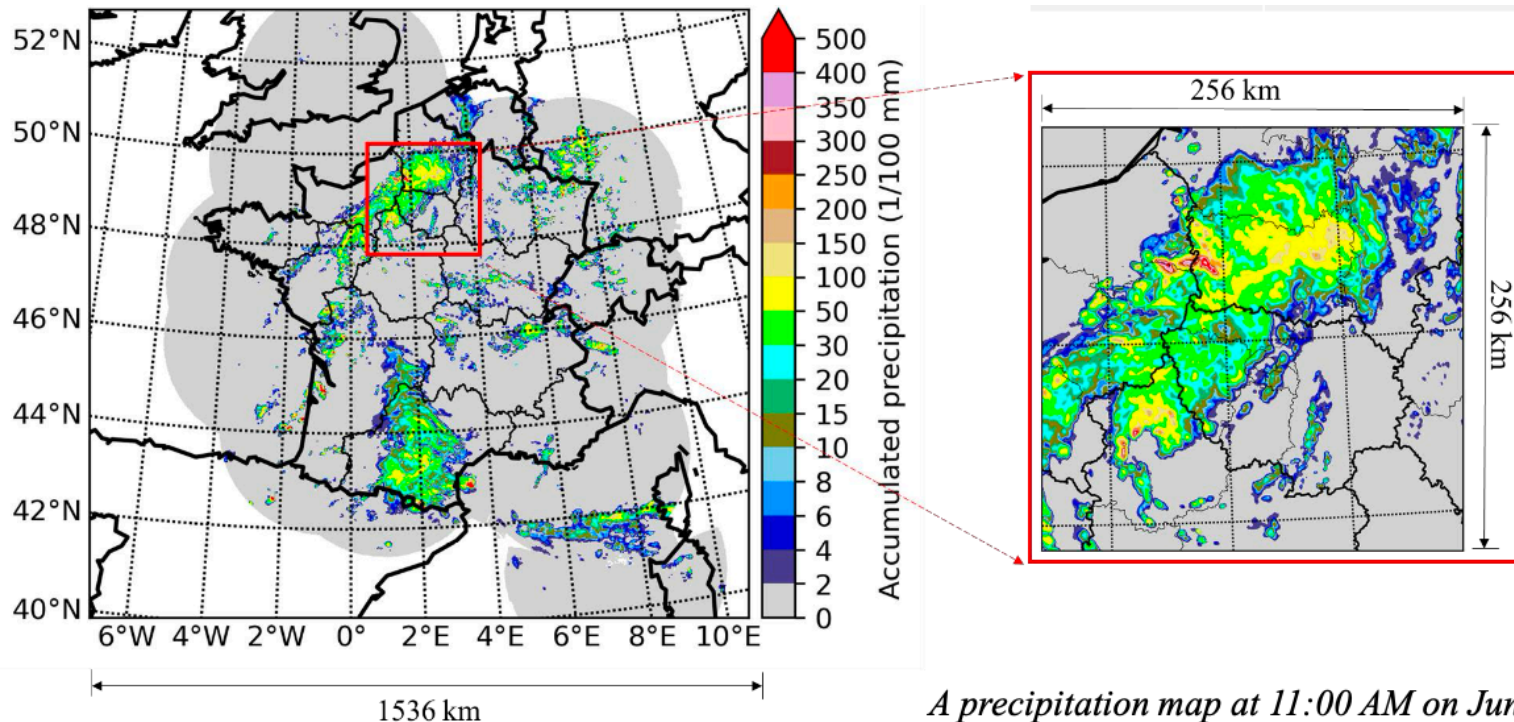
# Methodologies: Generative Adversarial Networks (GAN) model

- **Generative:** generate synthetic data
- **Adversarial:** a generator and a discriminator compete against each other, zero-sum game
  - the generator produces samples and try to fool discriminator
  - the discriminator distinguishes real and generated data
- **Networks:** convolutional neural network, ConvLSTM, fully connected network



# Precipitation nowcasting: dataset

- Data source: Météo-France<sup>1</sup>
- Accumulated precipitation (ACRR): the 5-minute rainfall in 1/100 mm
- Resolution: 5 min, 1 km



*A precipitation map at 11:00 AM on June 11, 2018*

Dataset	Period	Samples
Training	2018/01/01 - 2019/10/17	14014
Validation	2019/10/17 - 2019/12/24	3640

<sup>1</sup> thanks to Thibaut Montmerle and Yu Nan for suggestions and guidance

# Precipitation nowcasting: UM-GAN model process

Step1: Use **universal multifractals** to obtain three parameters in space and time.

Step2: **Generate space-time data** with 18 timesteps by continuous-in-scale multiplicative cascades, then to pick the 2D noise data at the lead times at 5min, 30min and 60min.

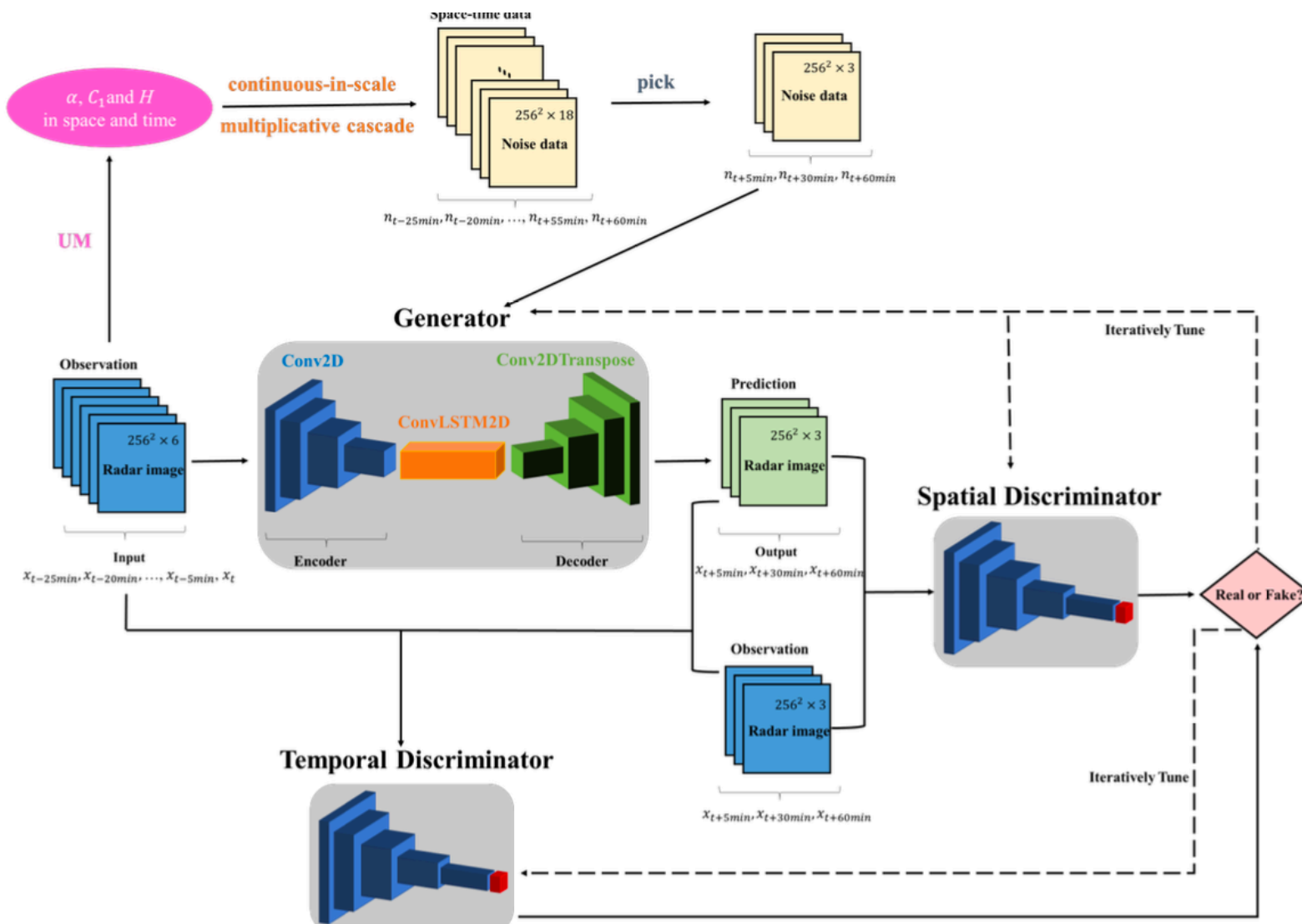
Step3: **Define UM-GAN architecture** based on the application of space-time nowcasting.

Step4: **Train the generator** to create predictions that try to fool two discriminators.

Step5: **Train the spatial discriminator and temporal discriminator** to distinguish real data from generated data in space and time.

Step 6: **Continue training** two discriminators and a generator alternately for multiple epochs.

Step7: **Save the best generator model** for creating predictions in the testing set.



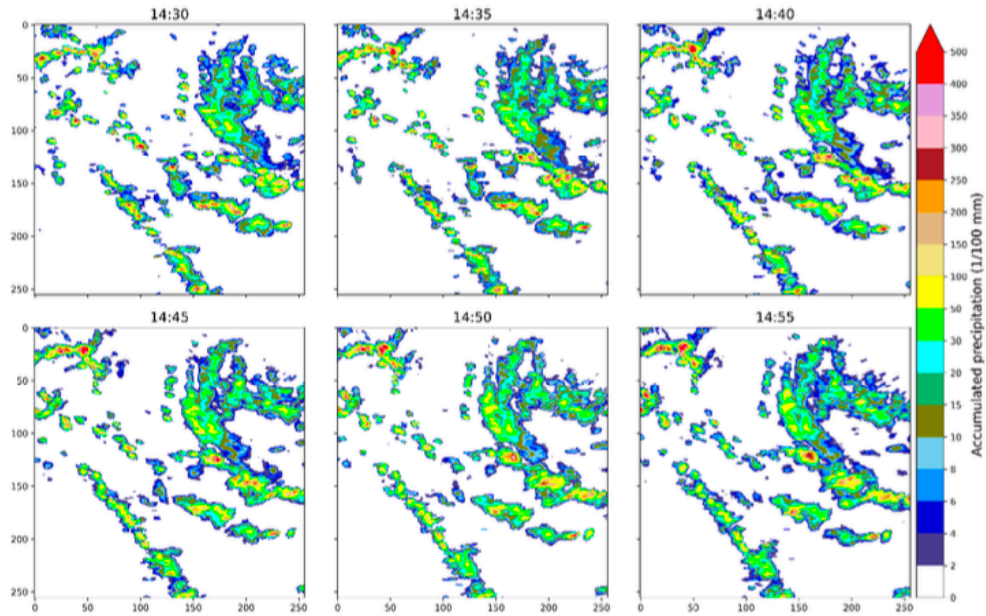
# Precipitation nowcasting: results analysis – Event 12/06/2020

**Description:** the thunderstorm with moderate rain due to a jet stream

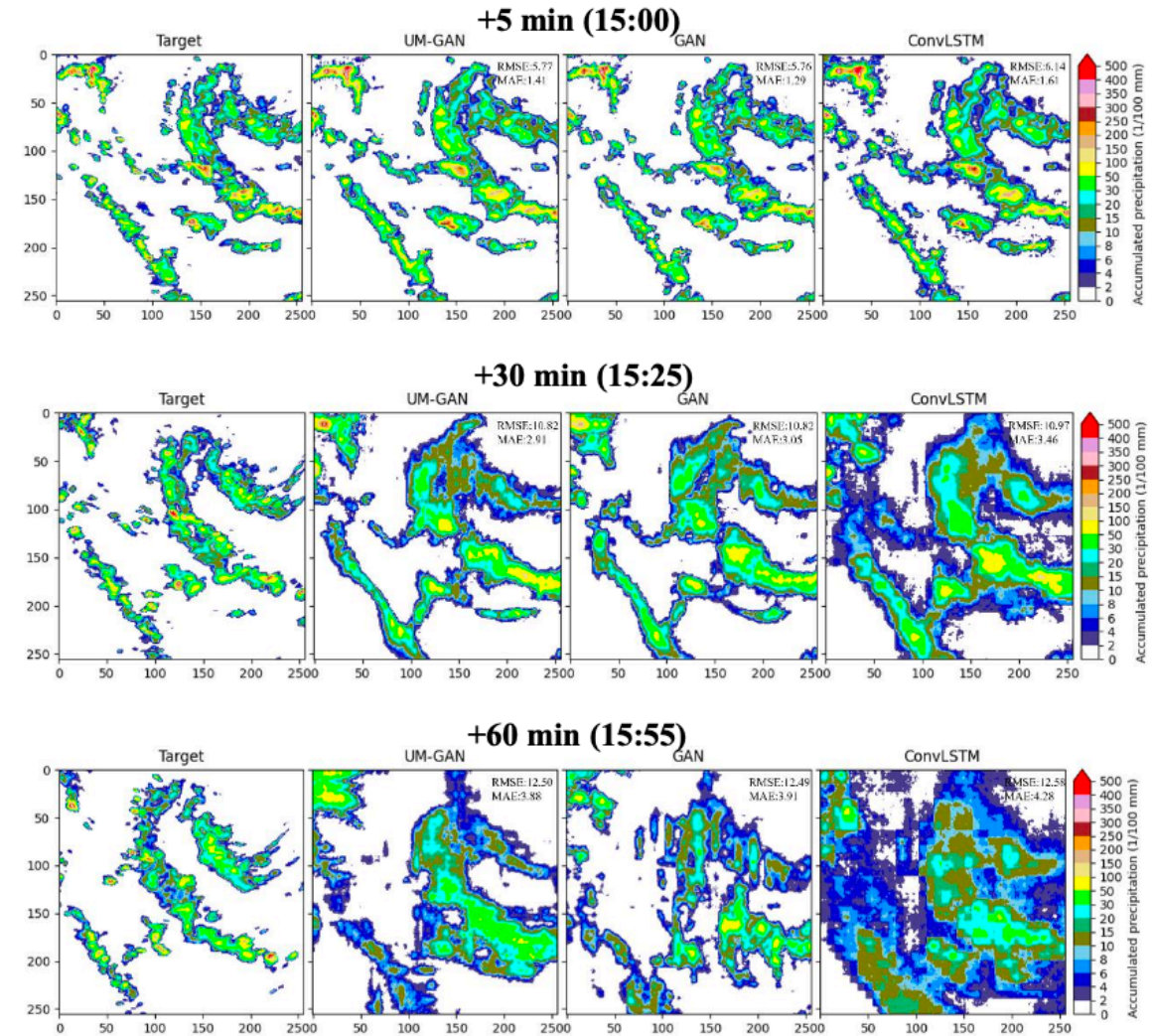
**Input :** previous 6 steps of historical data (14:30, 14:35, 14:40, 14:45, 14:50, 14:55); additional noise data generated by continuous-in-scale multiplicative cascades

**Output:** (15:00, 15:25, 15:55)

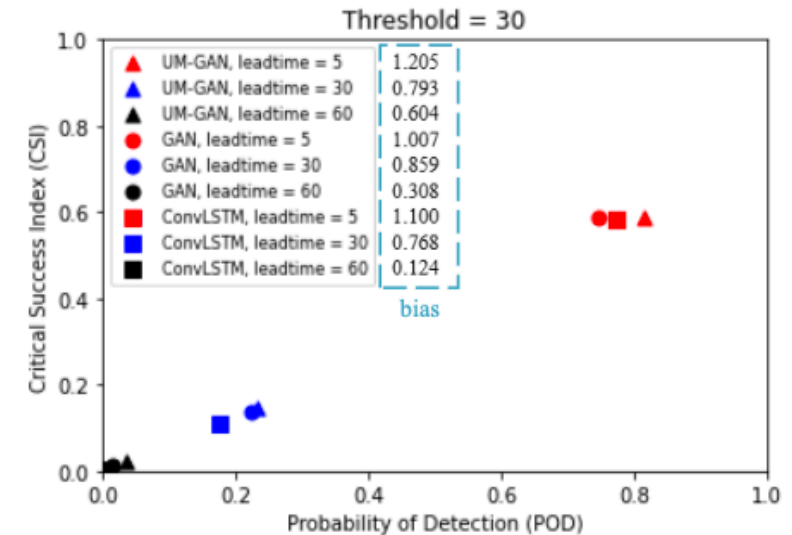
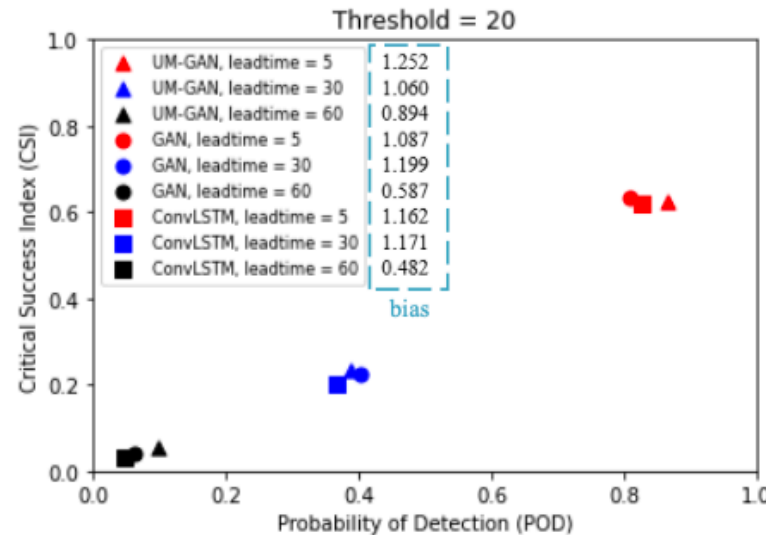
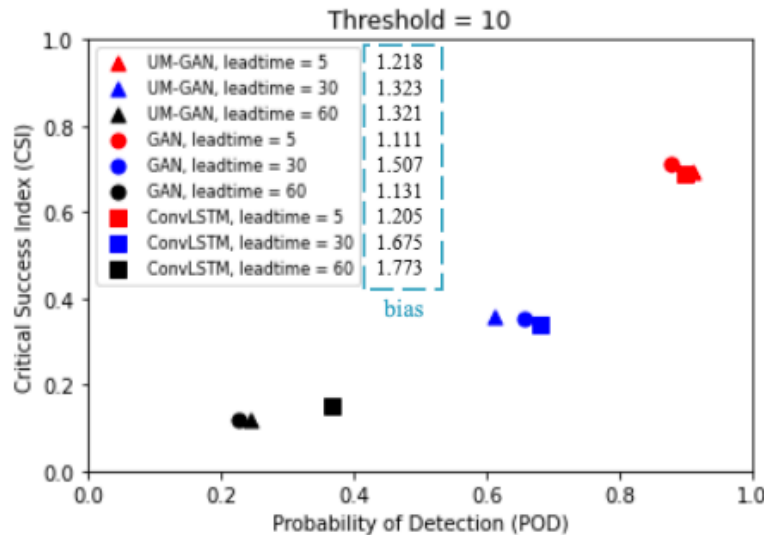
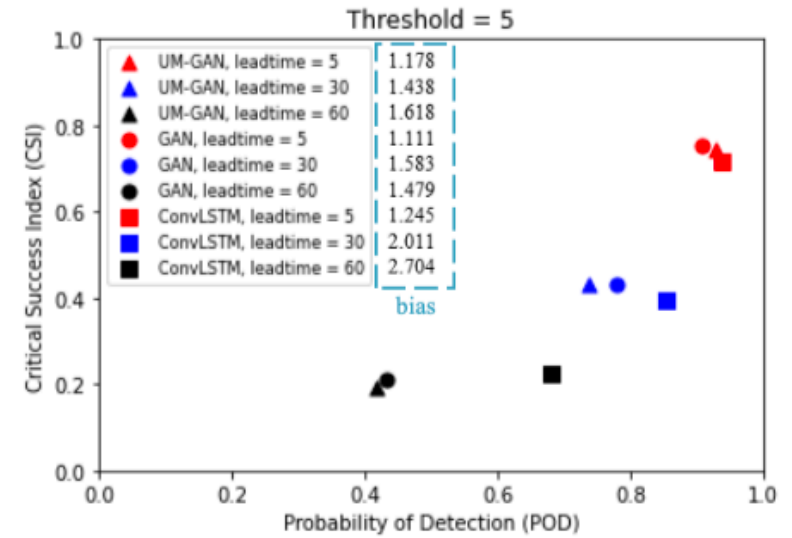
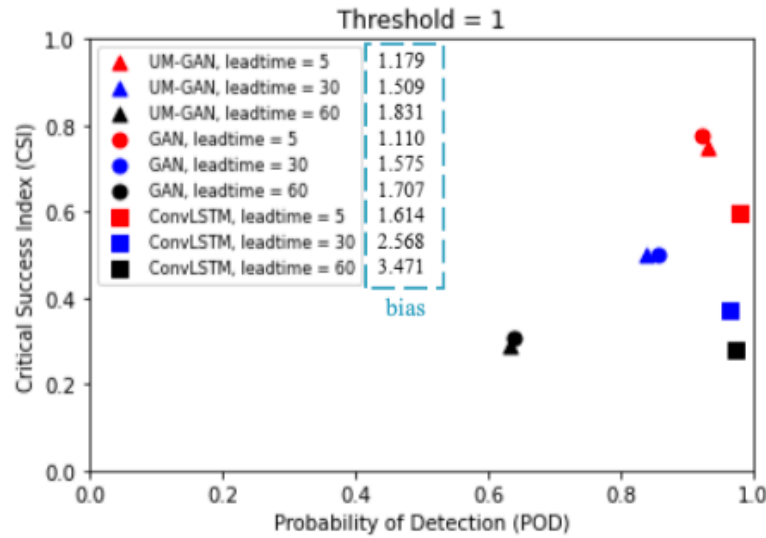
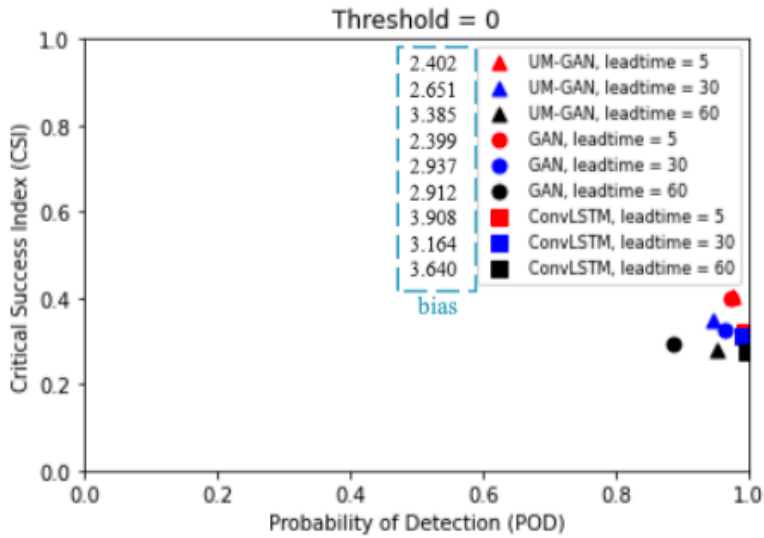
*The historical data from six previous time steps*



*Precipitation nowcasts by three different models and targets at the lead times of 5, 30 and 60 minutes*

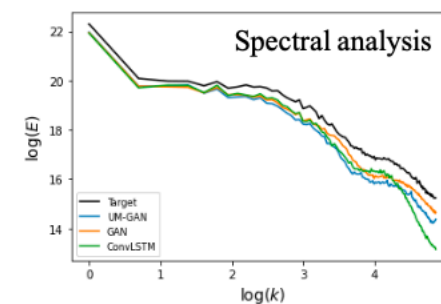
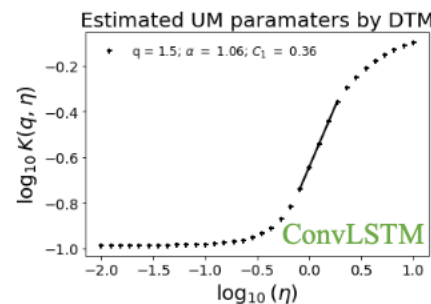
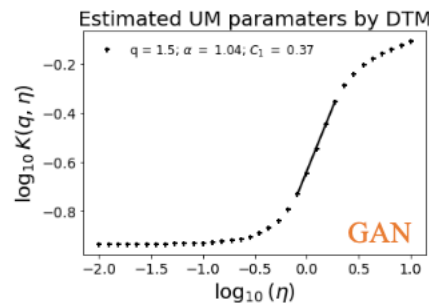
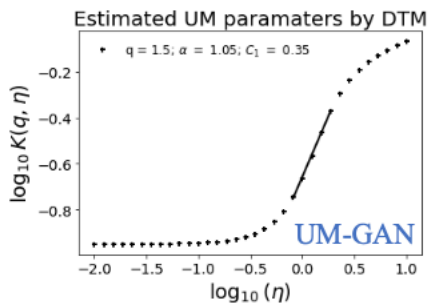
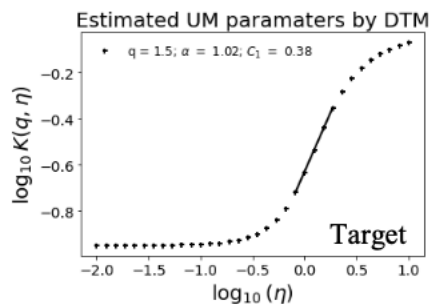


# Precipitation nowcasting: Categorical scores – Event 12/06/2020

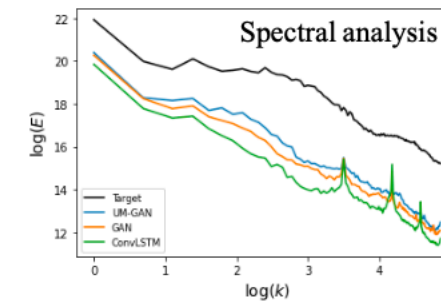
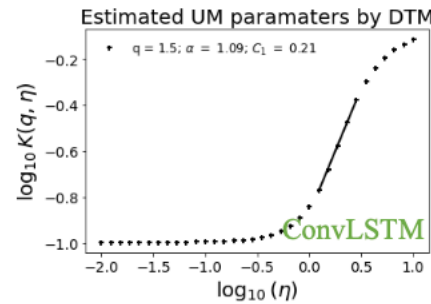
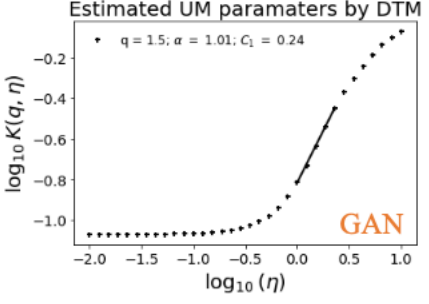
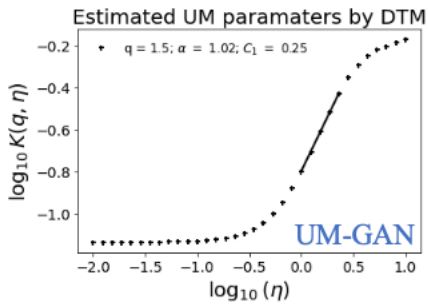
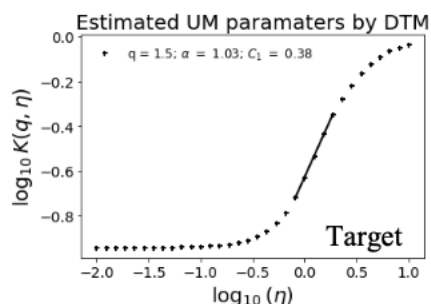


# Precipitation nowcasting: UM results – Event 12/06/2020

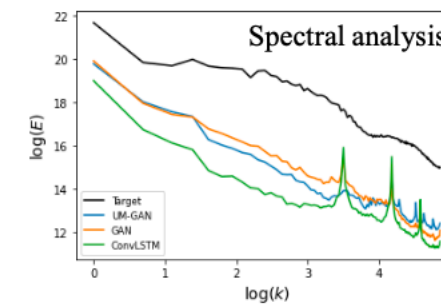
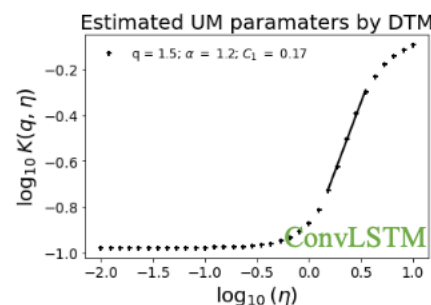
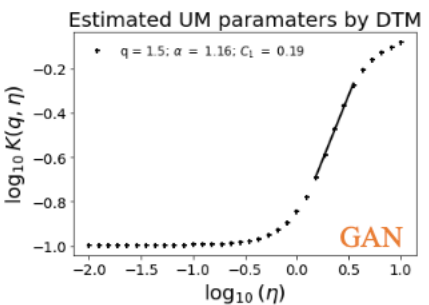
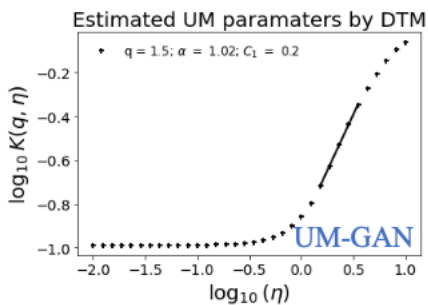
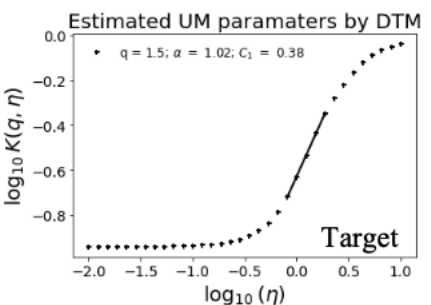
## at 5-minute lead time



## at 30-minute lead time



## at 60-minute lead time



# Conclusions and prospects

- **Conclusions**

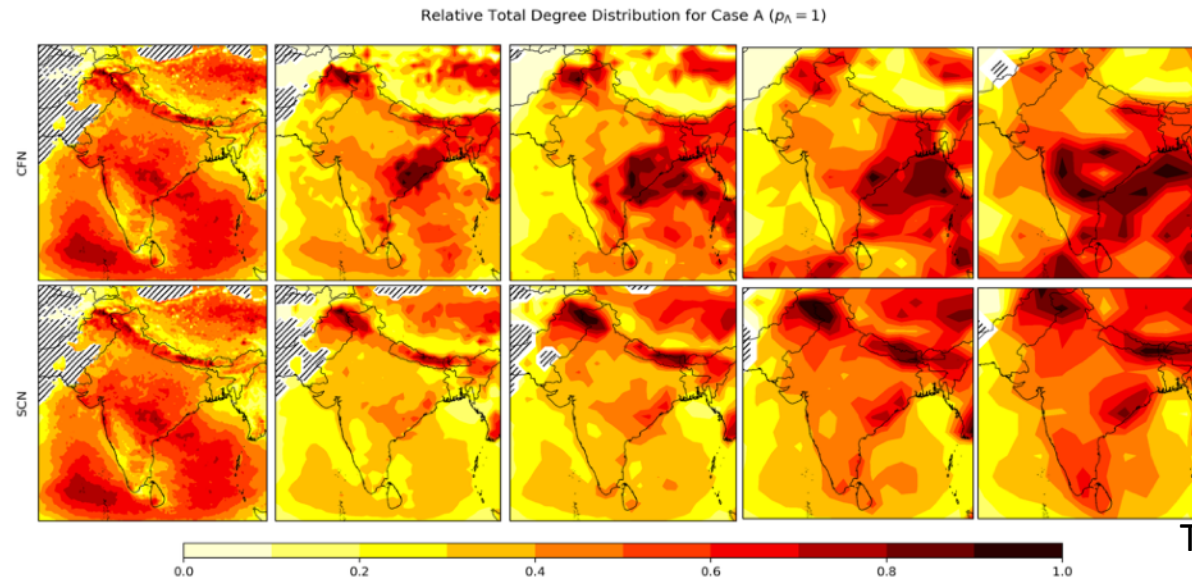
- VMD is effective for time series prediction (LSTM, GRU and bidirectional variants), but still underestimates extremes
- GAN-based models have better MAE and RMSE scores, and higher prediction accuracy in comparison to the ConvLSTM without adversarial training or linear regression
- stronger performance of UM-GAN in POD and CSI scores, and bias, particularly for thresholds of 10, 20, 30 (1/100 mm /5')
- UM parameters from ConvLSTM have a larger dispersion



# Conclusions and prospects

- **Prospects**

- increase accuracy of mean intermittency ( $C_1$ ) for longer lead times
- nowcasting of other geophysical fields
- multifractal prediction vs. RNN prediction (beyond GAN)
- neural networks and complex/climate networks
- ensemble predictions, or probabilistic versions



Thomas et al., EGU Letters. 2024